



5 September 2024 ELI ALPS Szeged Hungary

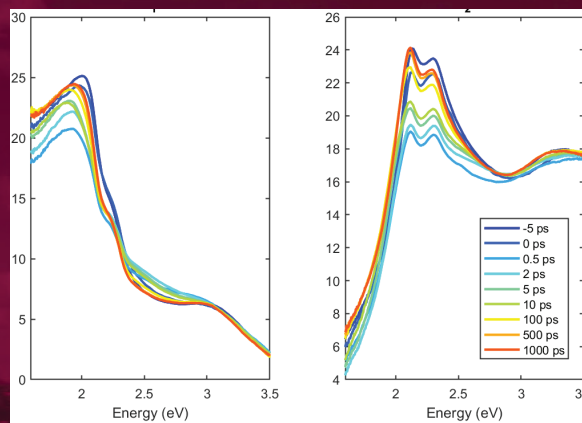
FA9550-20-1-0135 AFOSR
FA9550-24-1-0061 AFOSR

Relaxation, Band Filling, and Screening in the Transient Dielectric Function of Ge Determined with Femtosecond Ellipsometry

Stefan Zollner

in collaboration with:

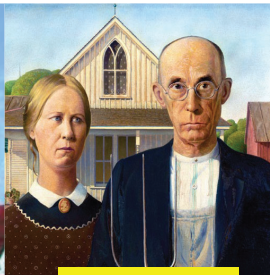
Carola Emminger, Carlos A. Armenta (NMSU)
Shirly Espinoza, Mateusz Rebarz, Martin Zahradnik,
Saul Vazquez-Miranda, Jakob Andreasson (ELI Beamlines)
Steffen Richter, Oliver Herrfurth, Rüdiger Schmidt-Grund
(Leipzig, Ilmenau)



Department of Physics, New Mexico State University, Las Cruces, NM, USA
Email: zollner@nmsu.edu. WWW: <http://femto.nmsu.edu>.

Biography

Regensburg/Stuttgart
Germany



Ames, IA

Motorola (Mesa, Tempe)
Arizona, 1997-2005



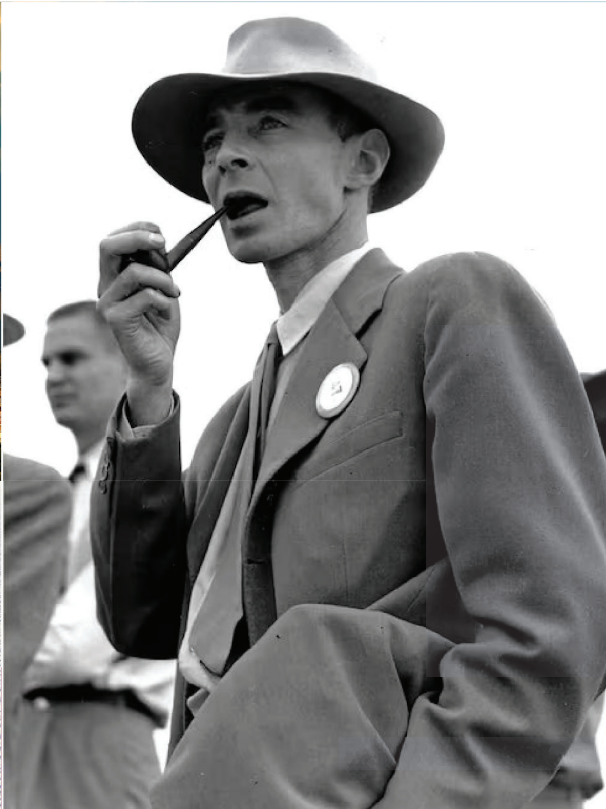
Freescle, IBM
New York, 91-92; 07-10

Motorola, Freescle
Texas, 2005-2007

NMSU
Las Cruces, NM
Since 2010



Where is Las Cruces, NM ???



When I was a kid, I thought that **if I could find a way to combine physics with New Mexico, my life would be perfect.**

My two great loves are physics and New Mexico. It's a pity they can't be combined.

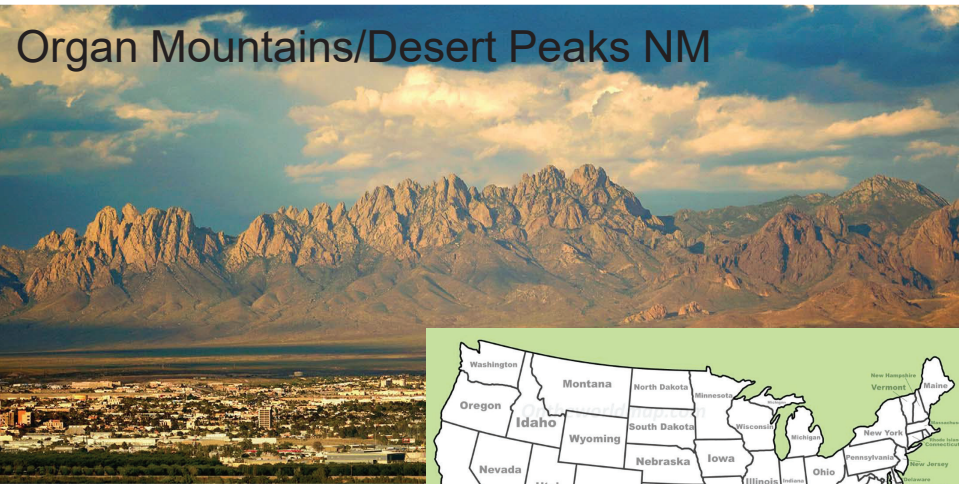
J. Robert Oppenheimer

Note: The NMSU Department of Physics was founded in 1934 by Prof. George Gardiner.

NP



Where is Las Cruces, NM ???



White Sands NP

Red or green chile peppers?

Green chile
Capsicum annuum

Ristra



Chile relleno



Red chile bowl



Green chile bowl

New Mexico State University, Las Cruces



Land grant institution, Carnegie R2 (soon to be R1)

Comprehensive: Arts and Sciences, Education, Business, Agriculture
Ph.D. programs in sciences, engineering, agriculture; Ag extension;

Chile Pepper Institute

12,700 students (11,000 UG, 1,700 GR), 1000 faculty

Minority-serving, Hispanic-serving (60% Hispanic/NA, 26% White)
Small-town setting (111,000)

Military-friendly institution (Army and Air Force ROTC programs)

Community engagement classification
(first-generation students, Pell grant recipients)

Physics: BS/BA, MS, PhD degrees. 67 UG and 39 GR students.
11 faculty (HE Nuclear and Materials Physics), **2.4 M\$ expenditures.**
ABET-accredited BS in Physics and BS in Engineering Physics

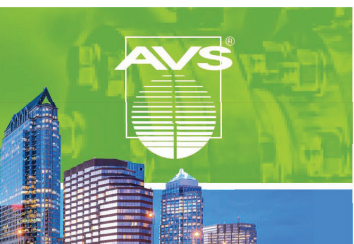


BE BOLD. Shape the Future.

Stefan Zollner, 2024

Problem statement

- (1) Achieve a **quantitative** understanding of **photon absorption** and **emission** processes.
- Our **qualitative** understanding of excitonic absorption is 50-100 years old (Einstein coefficients),
 - But **insufficient** for modeling of detectors and emitters.
- (2) How are optical processes affected by **high carrier concentrations** (screening)?
- High carrier densities can be achieved with
 - In situ doping or
 - **ultrafast (femtosecond) lasers** or
 - high temperatures (narrow-gap or gapless semiconductors)
 - **Application:** CMOS-integrated mid-infrared camera (thermal imaging with a phone).
 - Future: How are optical processes affected by an electric field (pin diode or thin layer)?



AVS 70th International Symposium & Exhibition Spectroscopic Ellipsometry

November 3-8, 2024 | Tampa, Florida | Call for Abstracts Deadline: **May 13, 2024**

Application: Midwave Infrared Detectors Germanium-Tin Alloys

Intensity of Optical Absorption by Excitons

R. J. Elliott
Phys. Rev. **108**, 1384 – Published 15 December 1957



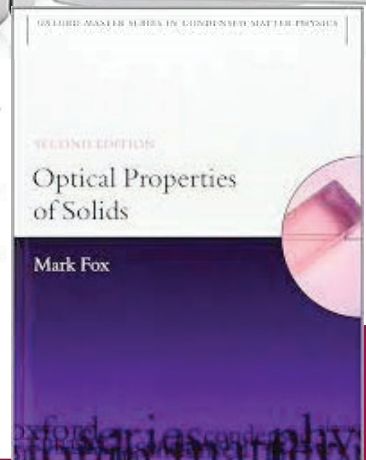
Article References Citing Articles (1,780) PDF Export Citation



ABSTRACT

The intensity of optical absorption close to the edge in semiconductors is examined using band theory together with the effective-mass approximation for the excitons. Direct transitions which occur when the band extrema on either side of the forbidden gap are at the same \mathbf{K} , give a line spectrum and a continuous absorption of characteristically different form and intensity, according as transitions between band states at the extrema are allowed or forbidden. If the extrema are at different \mathbf{K} values, indirect transitions involving phonons occur, giving absorption proportional to $(\Delta E)^{\frac{1}{2}}$ for each exciton band, and to $(\Delta E)^2$ for the continuum. The experimental results on Cu_2O and Ge are in good qualitative agreement with direct forbidden and indirect transitions, respectively.

Received 9 April 1957



Ellipsometry at NMSU

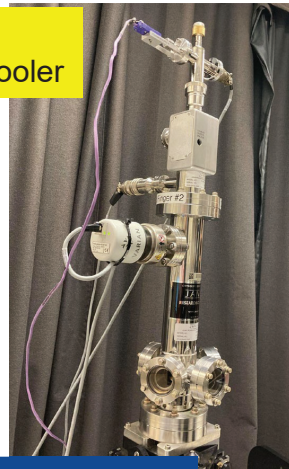
diamond windows
closed-cycle He cooler



Ellipsometry on anything (inorganic, 3D)

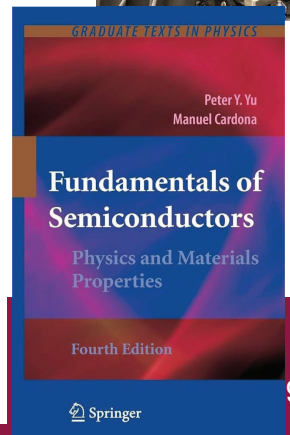
- Metals, insulators, semiconductors
- Mid-IR to vacuum UV (150 nm to 40 μm)
- **10 to 800 K, ultrafast ellipsometry**

Ellipsometry tells us a lot about materials quality (not necessarily what we want to know).



<u>Optical critical points of thin-film $\text{Ge}_{1-y}\text{Sn}_y$ alloys: A comparative $\text{Ge}_{1-y}\text{Sn}_y / \text{Ge}_{1-x}\text{Si}_x$ study</u>	440	2006
VR D'costa, CS Cook, AG Birdwell, CL Littler, M Canonico, S Zollner, ... Physical Review B—Condensed Matter and Materials Physics 73 (12), 125207		
<u>Growth and strain compensation effects in the ternary $\text{Si}_{1-x-y}\text{Ge}_x\text{C}_y$ alloy system</u>	397	1992
K Eberl, SS Iyer, S Zollner, JC Tsang, FK LeGoues Applied physics letters 60 (24), 3033-3035		
<u>Ge–Sn semiconductors for band-gap and lattice engineering</u>	335	2002
M Bauer, J Taraci, J Tolle, AVG Chizmeshya, S Zollner, DJ Smith, ... Applied physics letters 81 (16), 2992-2994		

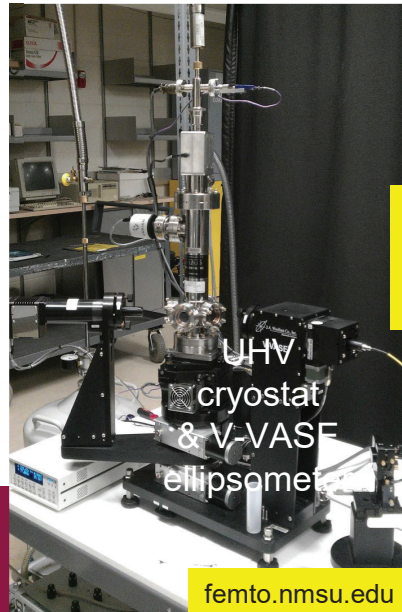
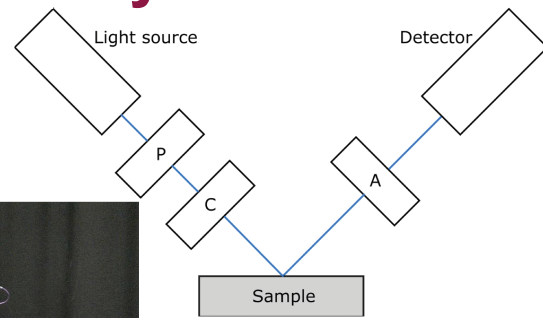
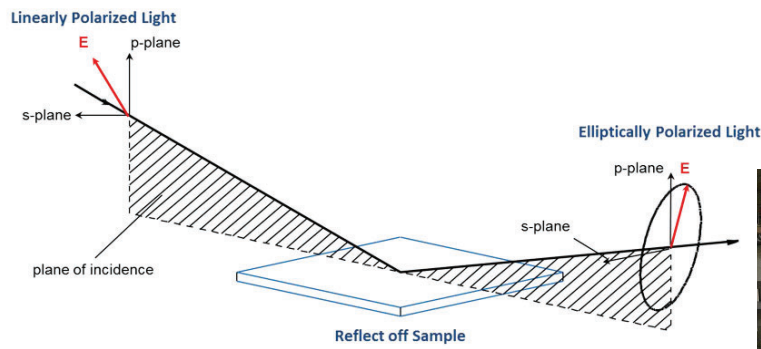
<http://femto.nmsu.edu>



Bandwidth considerations

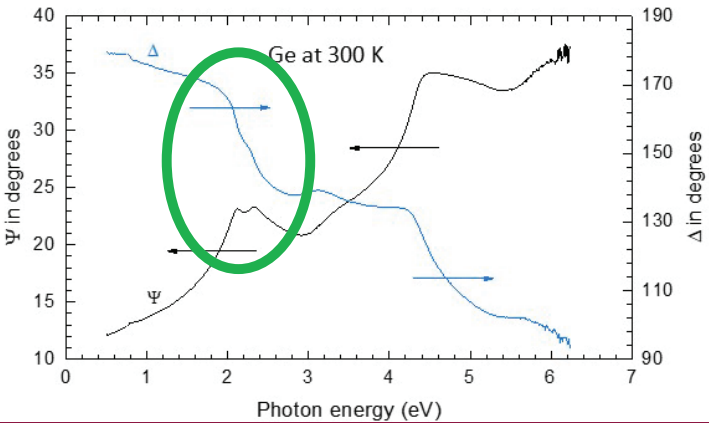
- **Heisenberg uncertainty principle:** $\Delta E \cdot \Delta t = \frac{\hbar}{2} = 330 \text{ meV} \cdot \text{fs}$
- **Attosecond spectroscopy:**
Low spectral resolution: 33 eV for 10 as pulse duration (use x-ray pulses)
High temporal resolution: Follow the real-space motion of electrons (and nuclei)
- **Femtosecond spectroscopy:**
Better spectral resolution: 33 meV for 10 fs pulse length
Minimal coherent artifacts (dephasing time smaller than pulse width)
Temporal resolution insufficient to follow the real-space motion of electrons.
Treat electrons and nuclei motion as waves: Reciprocal space (Brillouin zone of a crystal)
- **Molecular (or crystal) vibration spectroscopy (phonons):**
Requires high spectral resolution (1 meV or better): use picosecond pulses
- **Electronic state (band structure) spectroscopy (this work):**
Requires moderate spectral resolution (10 meV): use 30 femtosecond pulses (or longer)

Spectroscopic ellipsometry



ellipsometric angles ψ , Δ
 refractive index $n+ik$
 dielectric function ϵ

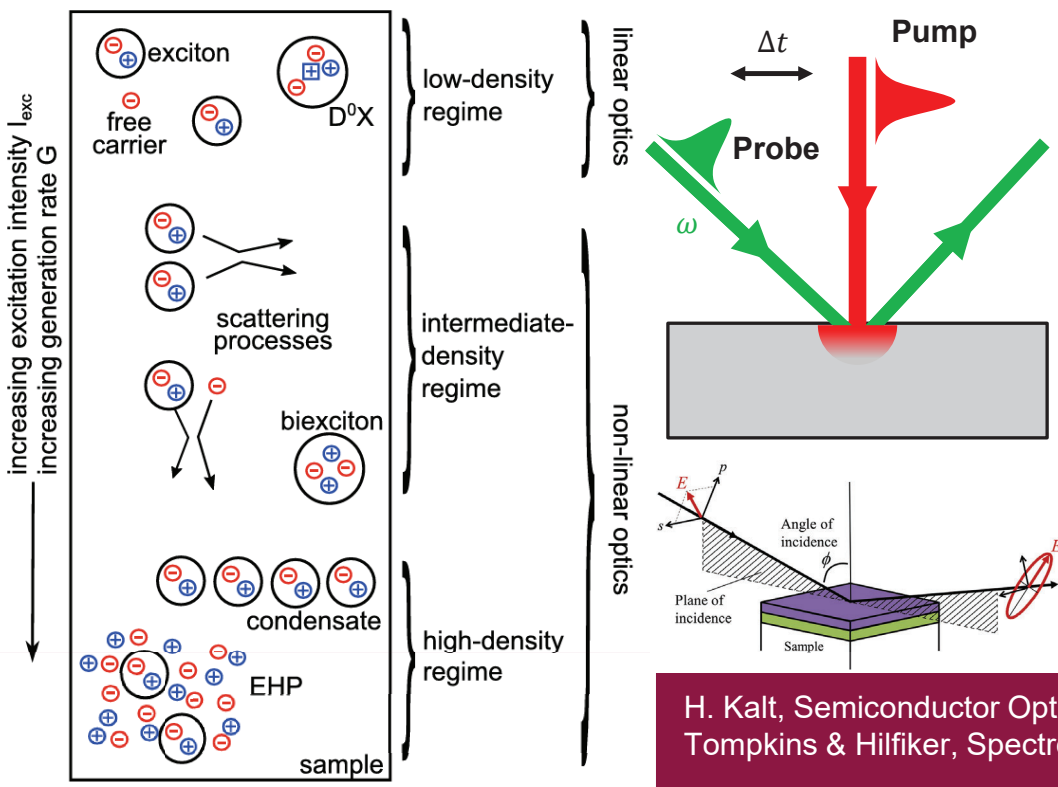
$$\rho = \frac{r_p}{r_s} = \tan \Psi e^{i\Delta}$$



Tompkins & Hilfiker,
 Spectroscopic
 Ellipsometry (2016)

femto.nmsu.edu

Femtosecond Pump-Probe Ellipsometry

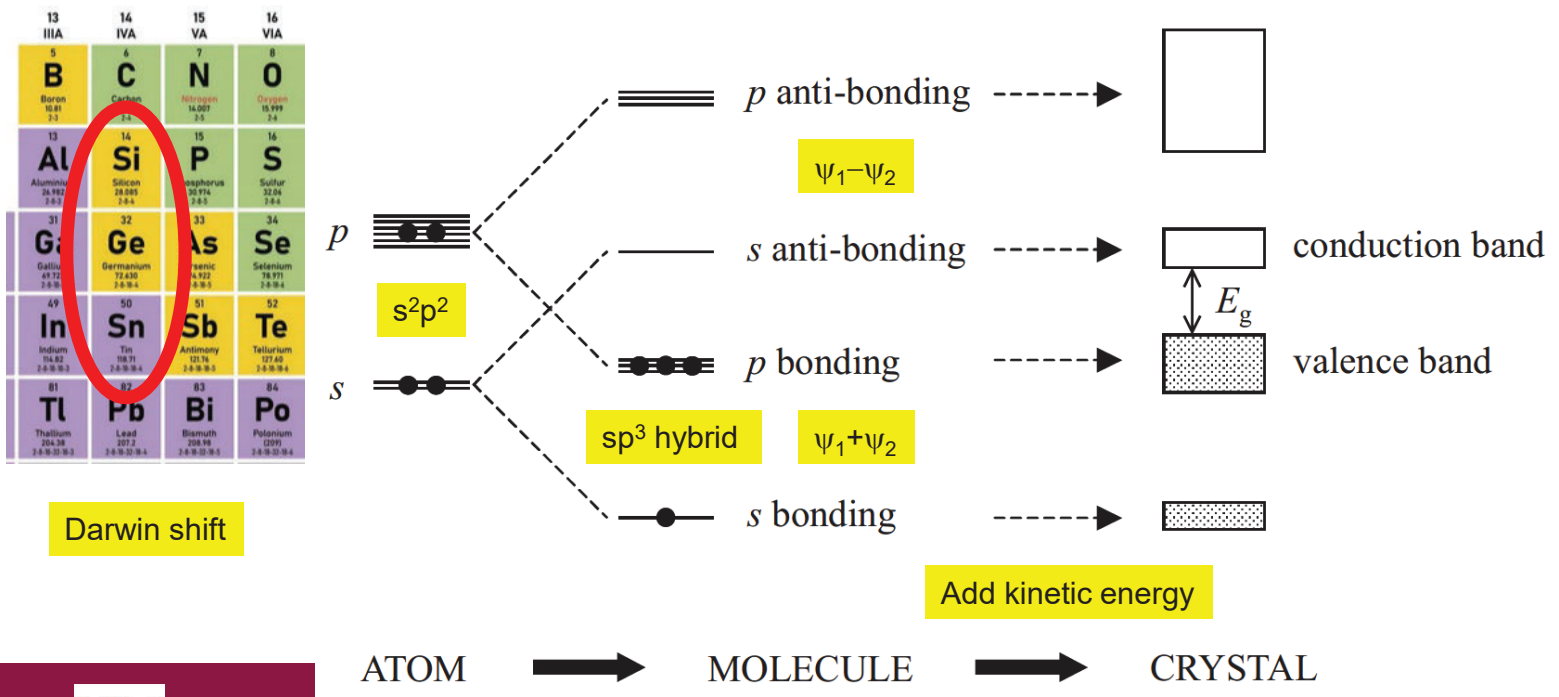


Non-linear effects in germanium induced by photoexcited carriers:

- Screening (many-body)
- Carrier-carrier scattering.
- Carrier-phonon scattering.
- Intervalley scattering.
- Momentum and energy relaxation of hot carriers.

H. Kalt, Semiconductor Optics 2 (2024).
 Tompkins & Hilfiker, Spectroscopic Ellipsometry (2016)

Ge Band structure: where did this come from?



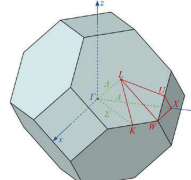
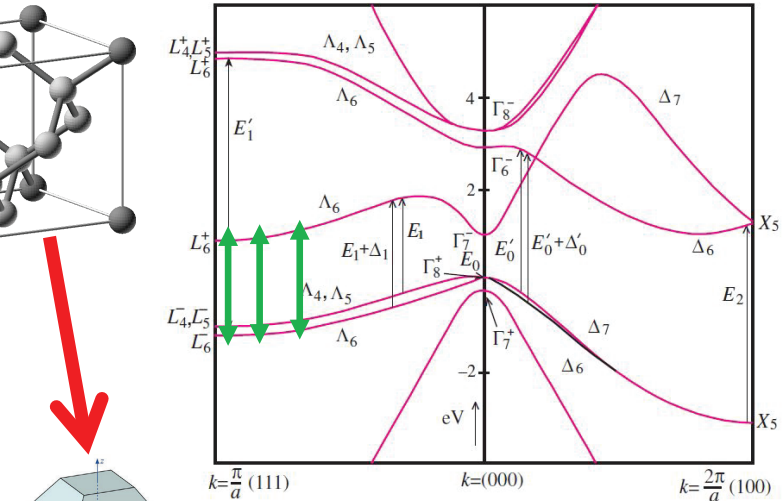
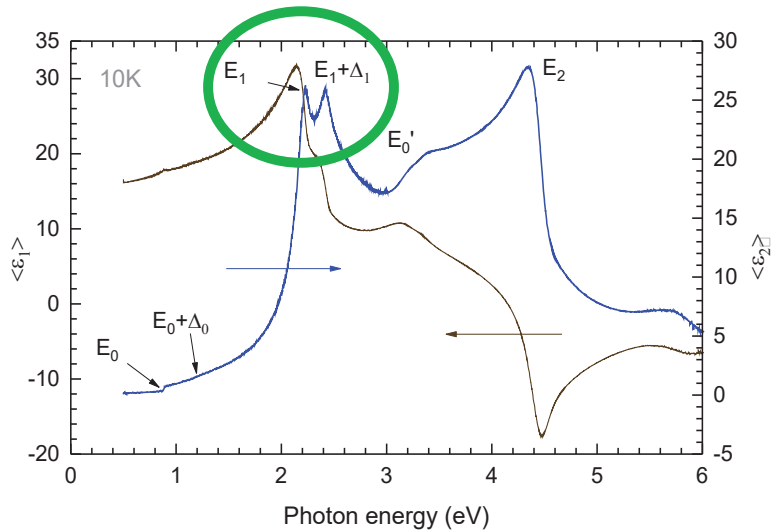
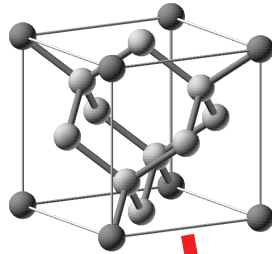
ATOM → MOLECULE → CRYSTAL

Works well for Ge, GaAs, etc.

Fox, Chapter 3

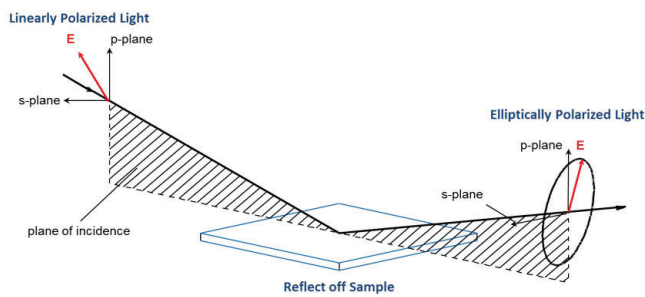
Critical points in the dielectric function of Ge

- Peaks in the dielectric function
- Due to interband transitions from valence to conduction band (electron-hole pairs)



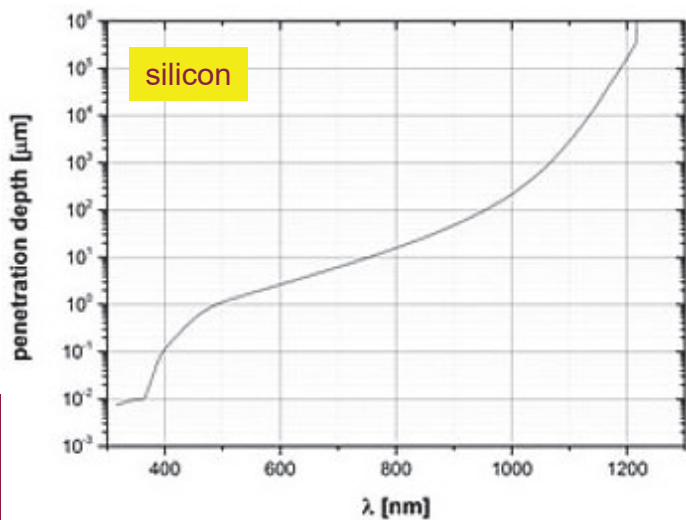
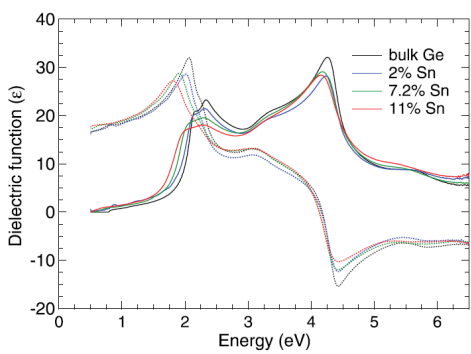
$$\psi(\vec{r}) = e^{i\vec{k}\cdot\vec{r}} u_{n,\vec{k}}(\vec{r})$$

Penetration depth

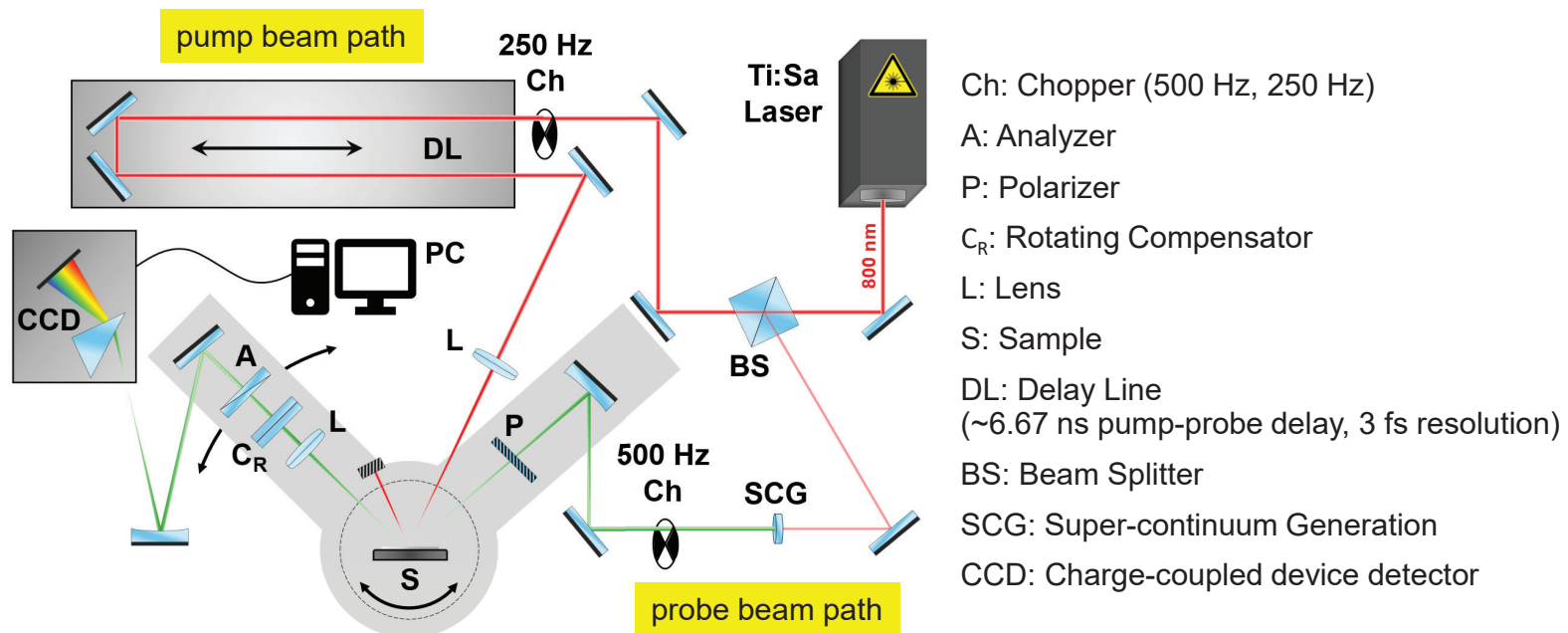


The penetration depth is the inverse of the absorption coefficient (measured with spectroscopic ellipsometry).

Below the direct band gap (0.8 eV for Ge, 3.4 eV for Si), the penetration depth is very large (many micrometers). The penetration depth is smallest at the E_2 peak in the UV, about 10 nm.

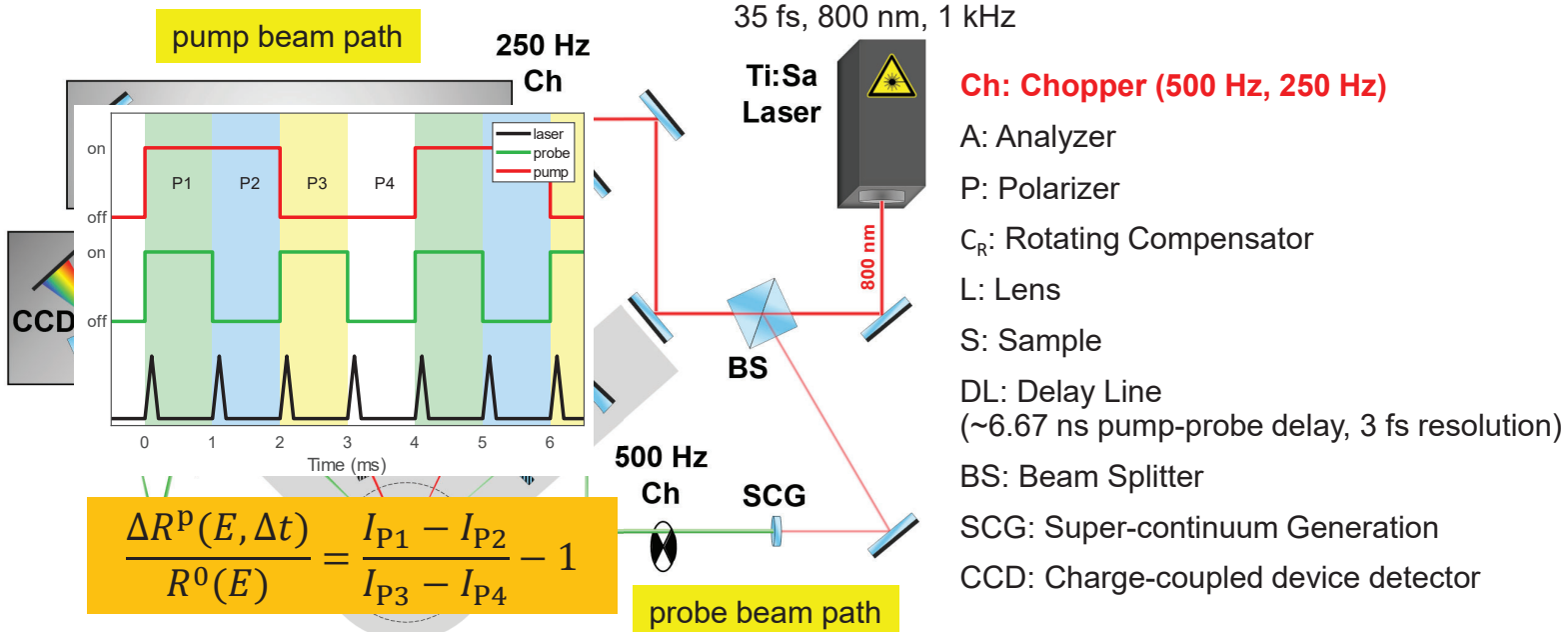


Experimental setup: pump-probe ellipsometry



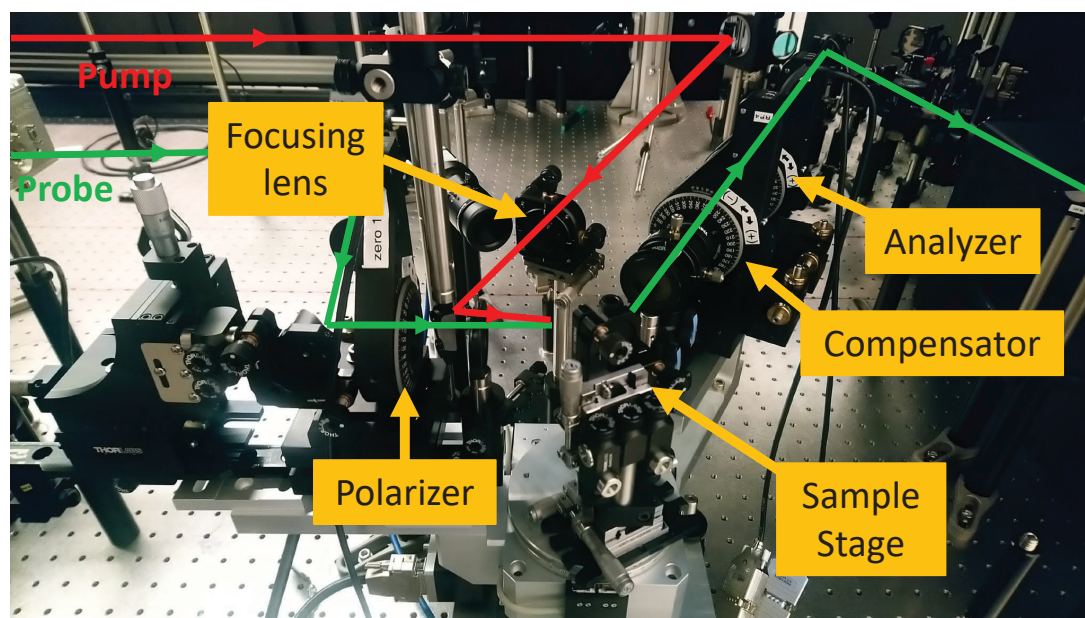
Experimental setup: pump-probe ellipsometry

35 fs, 800 nm, 1 kHz



$$\frac{\Delta R^P(E, \Delta t)}{R^0(E)} = \frac{I_{P1} - I_{P2}}{I_{P3} - I_{P4}} - 1$$

Set-up: Femtosecond pump-probe ellipsometry



Rotating compensator ellipsometer:

Compensator was rotated in steps of 10° for a total of 55-65 angles.

Probe beam of 350-750 nm at 60° incidence angle.

P-polarized pump beam: 35 fs pulses of 800 nm wavelength at 1 kHz repetition rate.

Delay time from -10 to 50 ps.

Time resolution of about 500 fs.

Femtosecond pump-probe ellipsometry at ELI ALPS

Pump

The femtosecond ellipsometer at ELI ALPS is similar, with some differences:

- Better time resolution (10 fs)
- Smaller spot size (10 μm)
- **Pump and probe with the same laser beam**
- No white light continuum probe
- Simpler setup

Rotating compensator ellipsometer:

... was rotated in steps of total of 55-65 angles.

... of 350-750 nm at 60° angle.

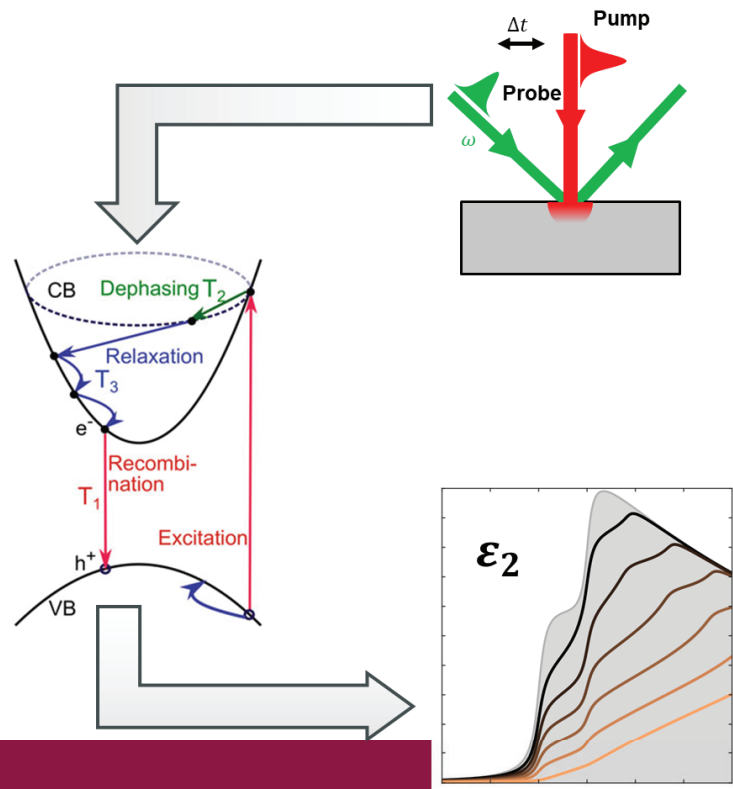
... pump beam: 35 fs 400 nm wavelength at 1 kHz repetition rate.

... from -10 to 50 ps.

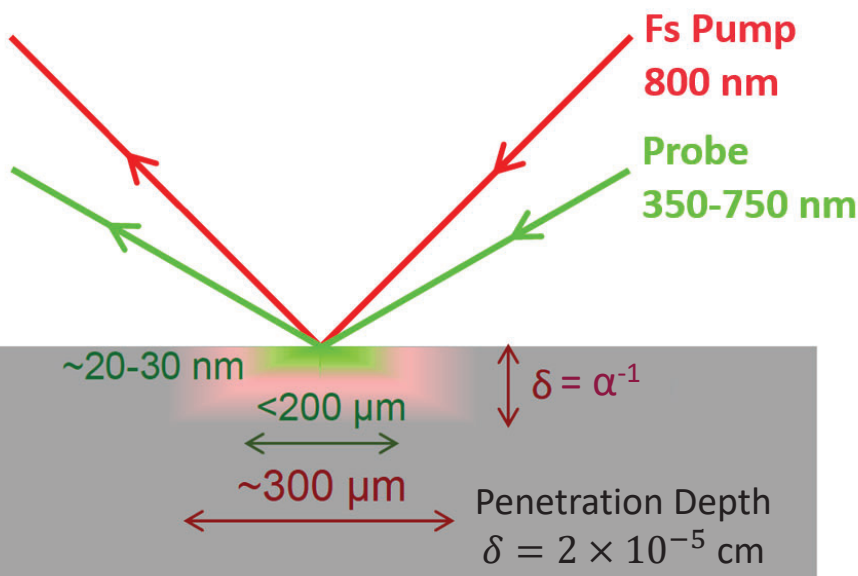
Time resolution of about 500 fs.

Outline

- Introduction:
- Experimental set up and procedure.
- Pump-pulse absorption and charge carrier density.
- Raw data.
- Ultrafast dynamics:
- Scattering processes and carrier statistics.
- Preliminary results.
- Modeling additional absorption processes.
- Conclusion & future work



Absorption of pump energy: charge carrier density



Number of Incident Photons

$$N = \frac{E_{\text{pulse}}}{E_{\text{photon}}} = \frac{P/f}{\omega\hbar}$$



Absorbed Photons

$$N_{\text{absorbed}} = (1 - R_p(\theta, \lambda))N$$



Charge Carrier Density

$$\frac{N_{\text{absorbed}}}{V} = \frac{N_{\text{absorbed}}}{A\delta}$$

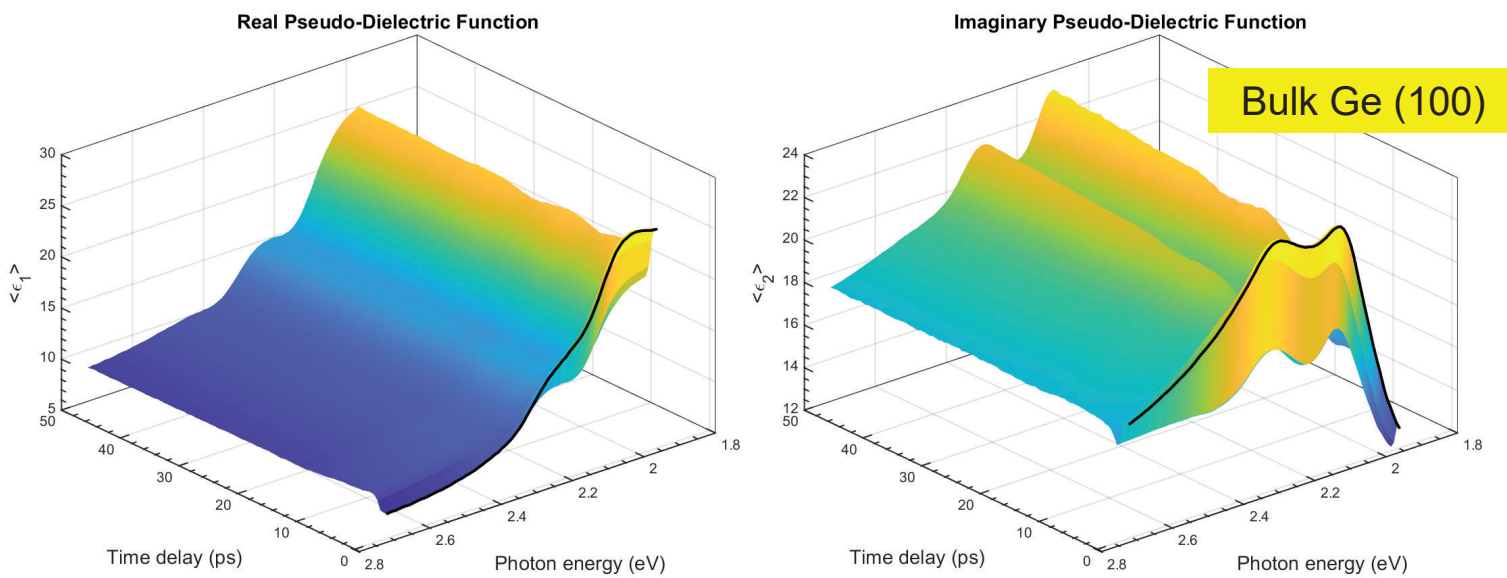
Absorption of pump energy: charge carrier density

Charge Carrier Density						
(Orientation) Pump Intensity	Bulk Ge (111)	Bulk Ge (110)	Bulk Ge (100)	nDoped Ge film*	GeSn Film (10% Sn)	GeSn Film (18% Sn)
Pump Power (mW) Pulse Energy (μJ)	13	14	3	2.5	2	5
Pump Beam Diameter (μm)	295	295	180	261	269	517
Charge Carrier Density (cm^{-3})	3.42×10^{21}	3.69×10^{21}	3.16×10^{21}	5.93×10^{20}	7.62×10^{20}	1.31×10^{20}

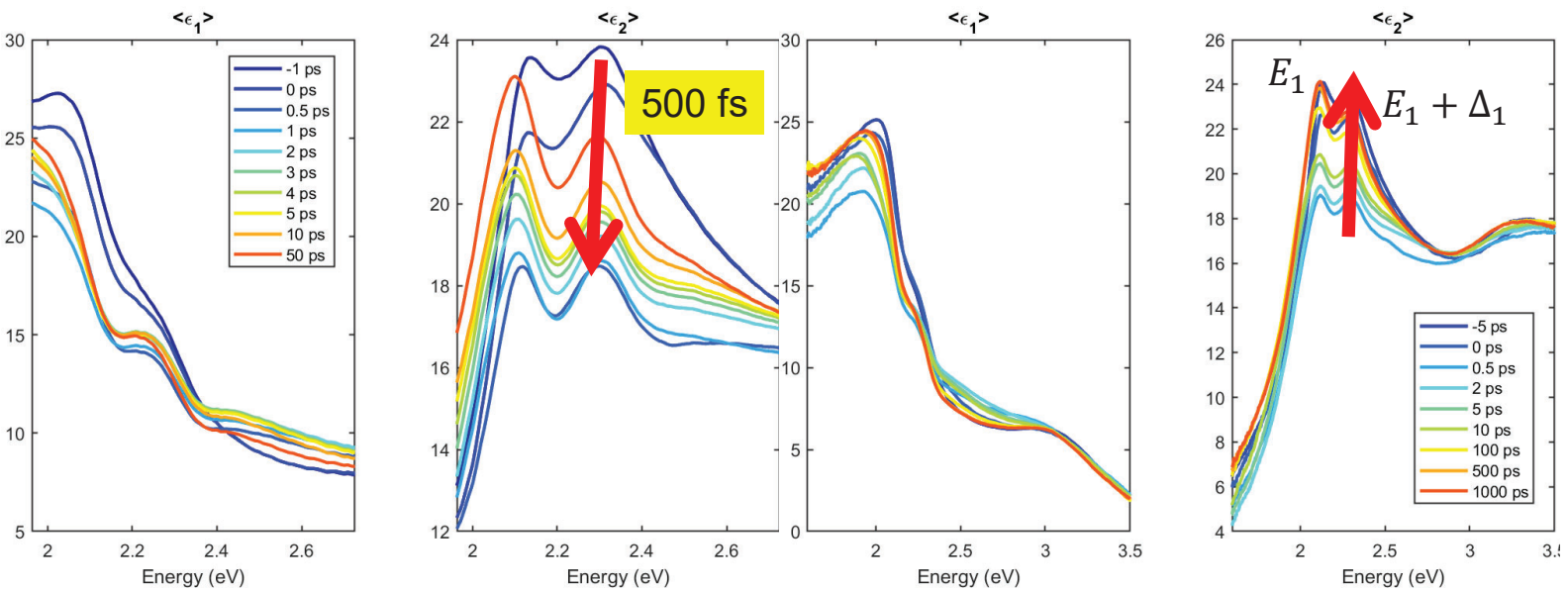
Excitation density just below the damage threshold.
Carrier concentration of $3 \times 10^{21} \text{ cm}^{-3}$ is not physical.
 The absorption is already bleached by the pump pulse.

* Doping: $n = 1.05 \times 10^{20} \text{ cm}^{-3}$

Pseudo-dielectric constant as function of delay time



Pseudo-dielectric constant as function of delay time



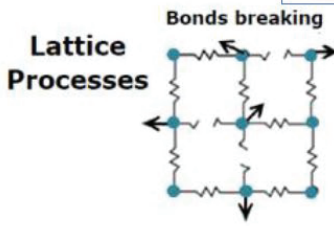
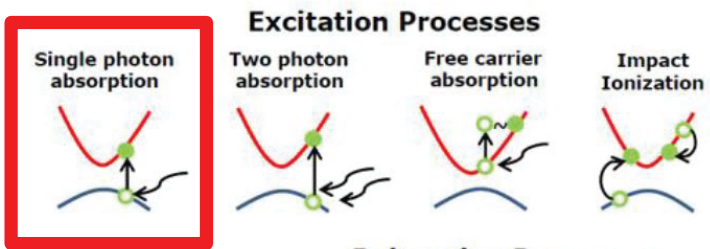
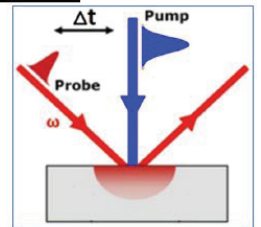
Rapid decrease of ϵ within first 500 fs.

Recovery takes 1 ns or longer.

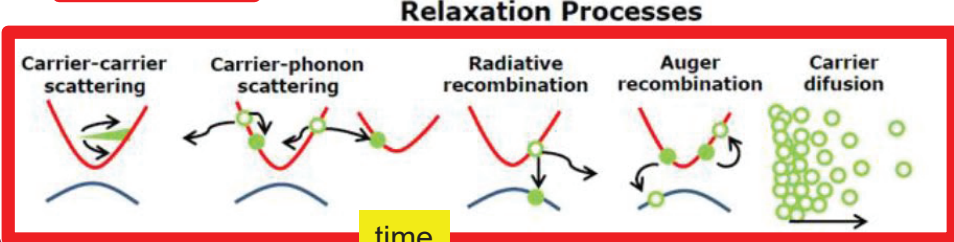
What is happening on these time scales ?



Shirly Espinoza



Excitation density below damage threshold.



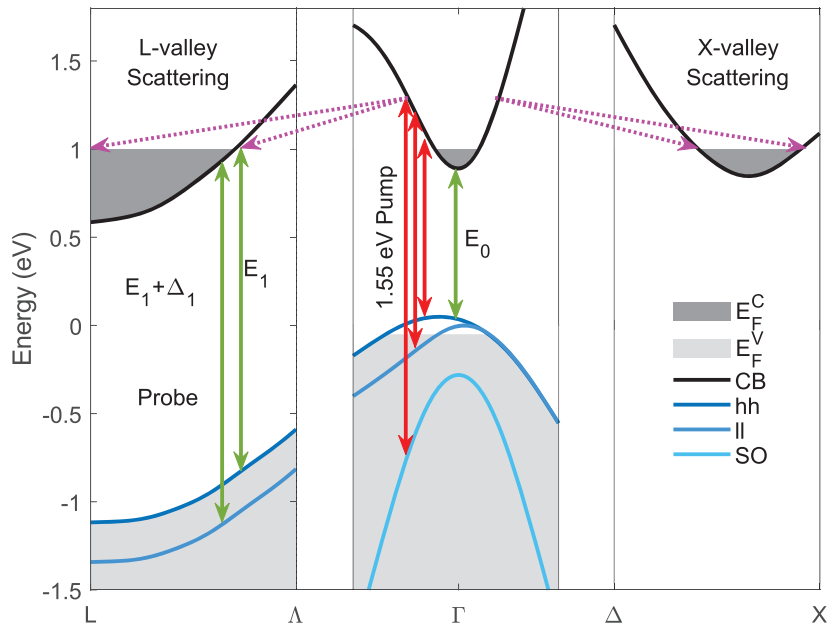
time



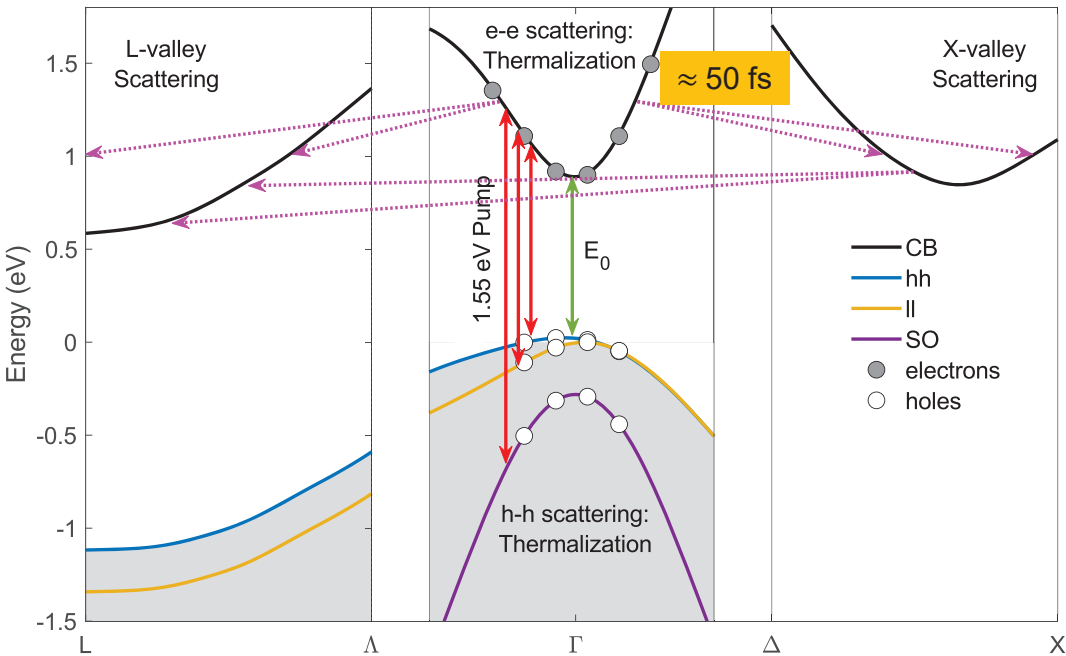
Interband transitions in Ge

- Generation of hot electrons in the Γ -valley with excess energy ϵ (≈ 0.7 eV).
- Momentum relaxation and thermalization of hot electrons (< 100 fs).
- Energy relaxation by intervalley scattering (GaAs: Γ to X: 50 fs).
- Optical functions change as a function of the density and energy of the electrons.
- Many-body phenomena affect the band transition energy:

$$\Delta E = \Delta E_{str} + \Delta E_{BM} + \Delta E_{BGR}$$



Carrier relaxation (<100 fs): Energy transfer to lattice



$$\varepsilon = \frac{\hbar\omega_{\text{pump}} - E_0}{1 + m_e/m_h}$$

Plasma temperature:

$$T_c \approx \frac{\varepsilon}{3k_B}$$

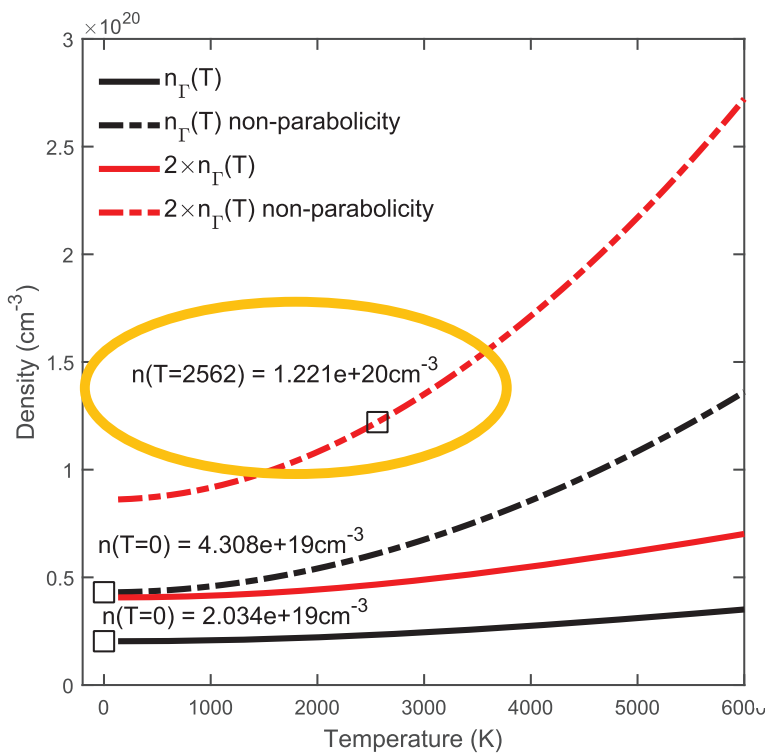
$$\varepsilon = 0.7 \text{ eV}$$

$$T = 2500 \text{ K}$$

Intervalley scattering is more efficient than intravalley scattering.

Stefan Zollner, Sudha Gopalan, and Manuel Cardona, Effective **deformation potentials** in the description of time-resolved and hot-electron luminescence, *Solid-State Commun.* **76**, 877-879 (1990)

Electron concentration from density of states



To avoid bleaching of the absorption, the chemical potential μ cannot be larger than the excess electron energy ε . Assume

$$\mu = \varepsilon + E_0$$

$$n_{\Gamma}(T) = \frac{1}{4} \left(\frac{2m_{e,\Gamma}k_B T}{\pi \hbar^2} \right)^{3/2} F_{1/2} \left(\frac{\varepsilon}{k_B T} \right)$$

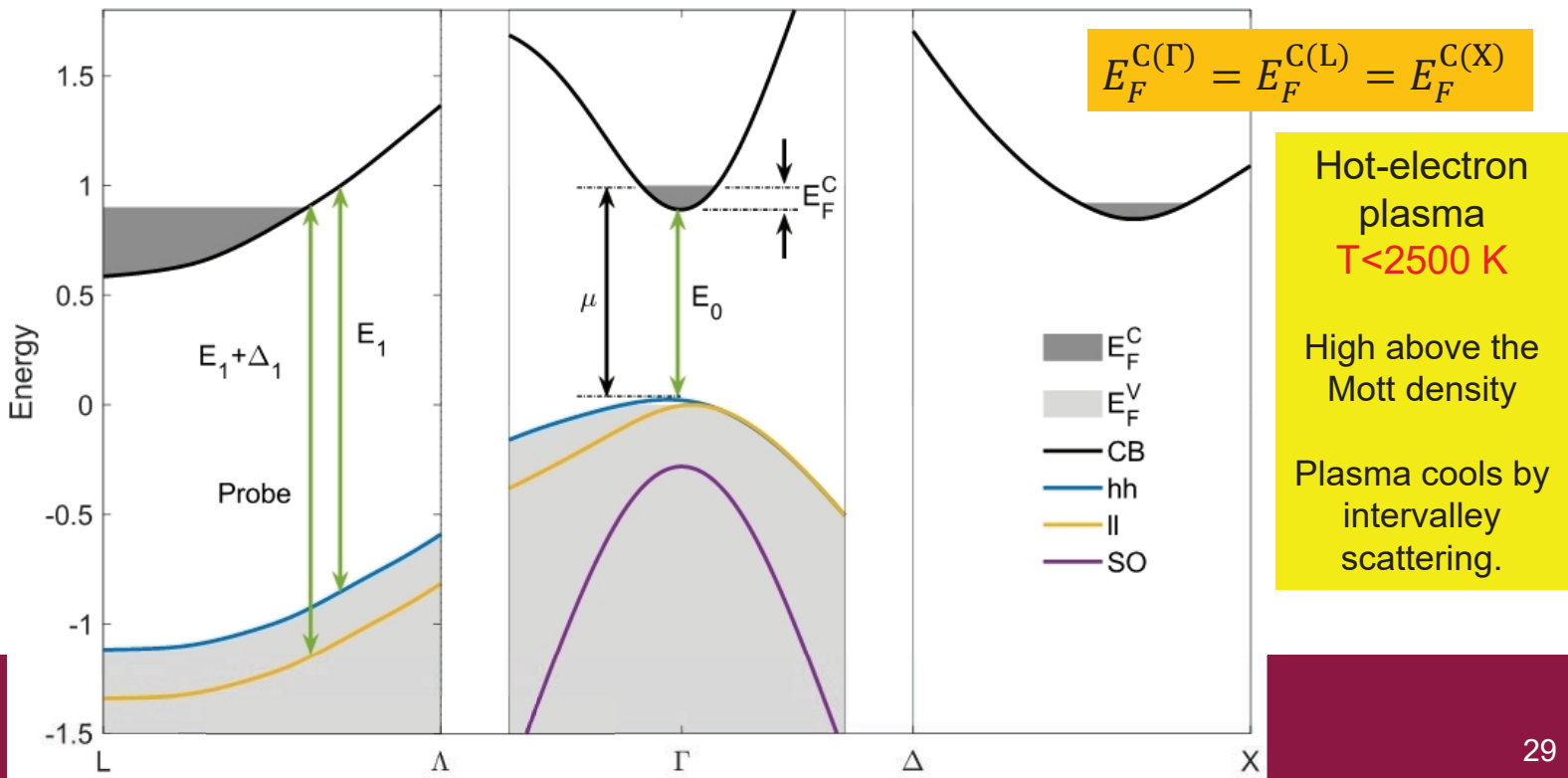
Calculate maximum electron concentration with Fermi-Dirac statistics:

n cannot be more than 10^{20} cm^{-3} .

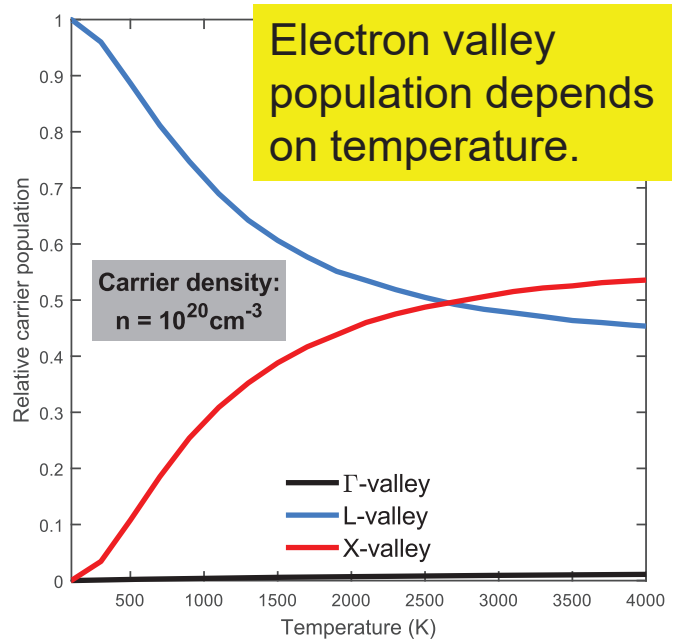
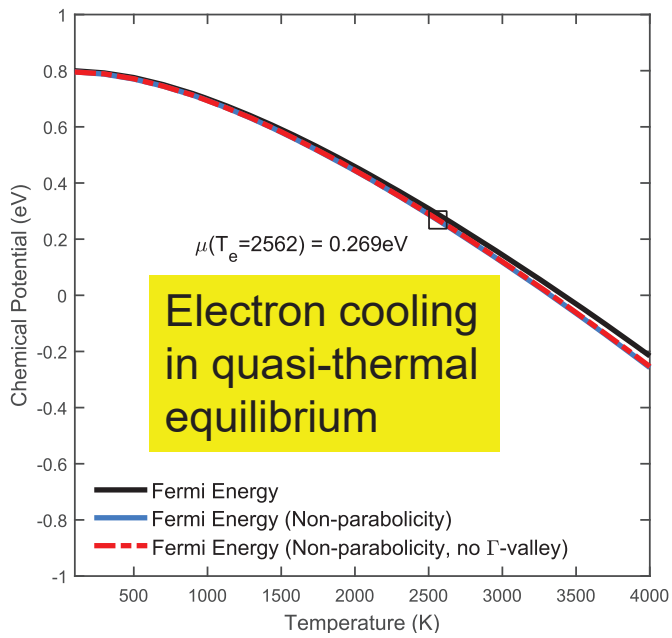
High above the Mott density (10^{17} cm^{-3}).

Consider density of states with conduction band non-parabolicity from k.p theory.

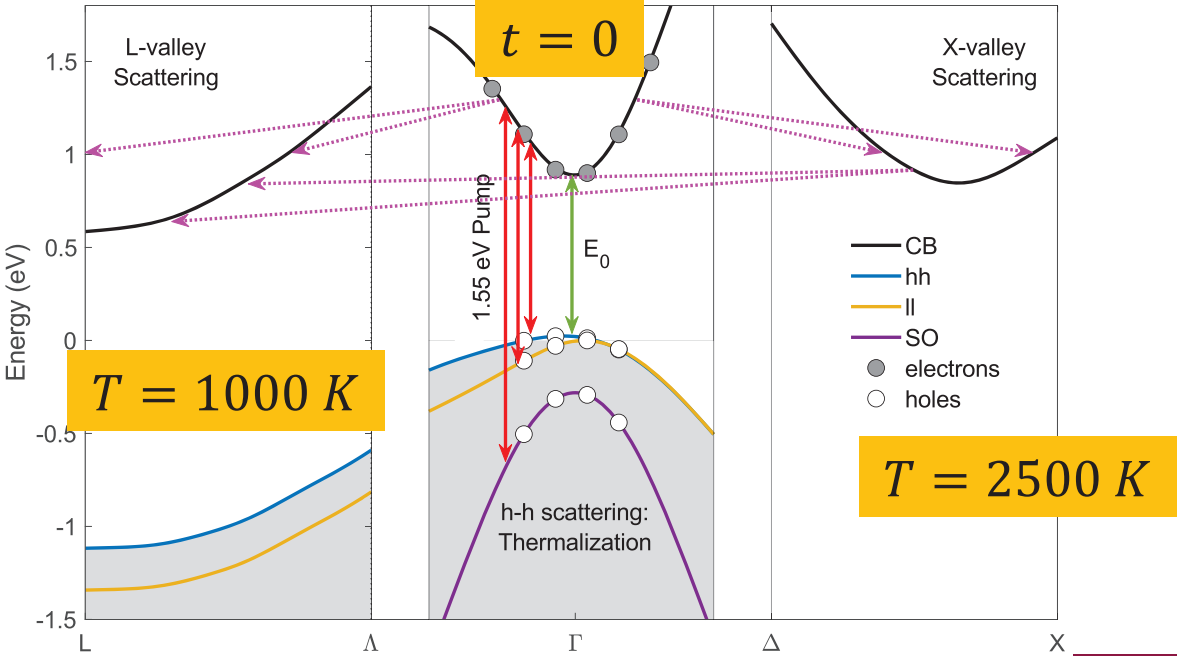
Thermal equilibrium between valleys (>500 fs)



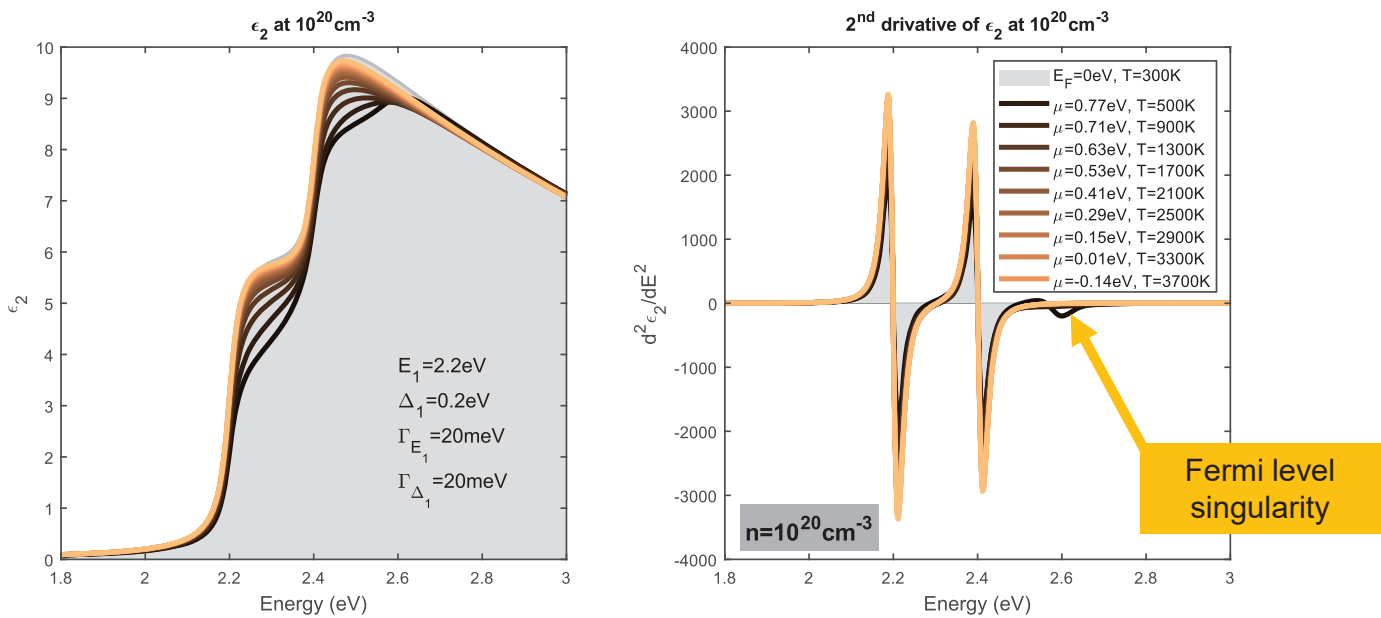
Electrons cooling by intervalley scattering (>500 fs)



Electrons cooling by intervalley scattering (>500 fs)



Band-filling model for transient dielectric function



$$\epsilon_2(E) = \frac{2e^2 \bar{P}^2 \mu_{\perp}}{3\pi \epsilon_0 m^2 E^2} H(E - E_1) \int_{-k_{\max}}^{k_{\max}} 1 - f[E_c(E, k_z^2)] dk_z$$

Xu, JAP **125**, 085704 (2019).
 Xu, PRL **118**, 267402 (2017).

Band-filling model for transient dielectric function

$$\varepsilon_2(E) = \frac{2e^2 \bar{P}^2 \mu_{\perp}}{3\pi \varepsilon_0 m^2 E^2} H(E - E_1) \int_{-k_{\max}}^{k_{\max}} 1 - f[E_c(E, k_z^2)] dk_z$$

Introduce broadening Γ of interband transitions.

Integration over Fermi-Dirac distribution yields Fermi integral $F_{-1/2}$.

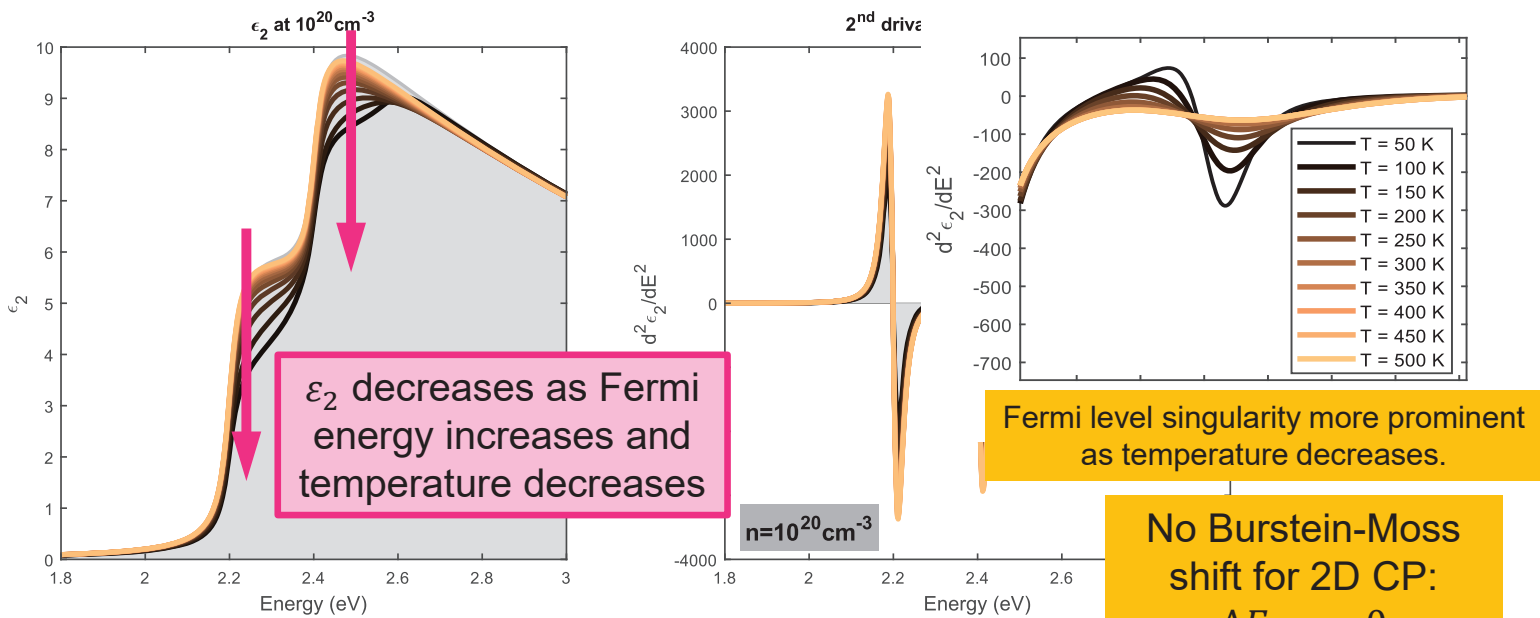
$$\varepsilon_2(E, \Gamma, \mu, T)$$

$$= \frac{1}{\pi} \text{Im} \left\{ \ln \left[\frac{2(E_1 - i\Gamma - E)}{E_1 - i\Gamma} \right] \right\} \frac{4k_{\max} e^2 \bar{P}^2 \mu_{\perp}^{(E_1)}}{3\pi \varepsilon_0 m^2 E^2} \left\{ 1 - \left(\frac{k_T}{2k_{\max}} \right) F_{-1/2} \left[\frac{\mu - (E - E_1) \frac{\mu_{\perp}}{m_{\perp}}}{k_B T} \right] \right\}$$

Fixed parameters: Band gap E_1 , momentum matrix element P , effective masses m_i , μ_i

Adjustable parameters: Broadening Γ , chemical potential μ , temperature T , wave vector range k_{\max}

Band-filling model for transient dielectric function



ϵ_2 decreases as Fermi energy increases and temperature decreases

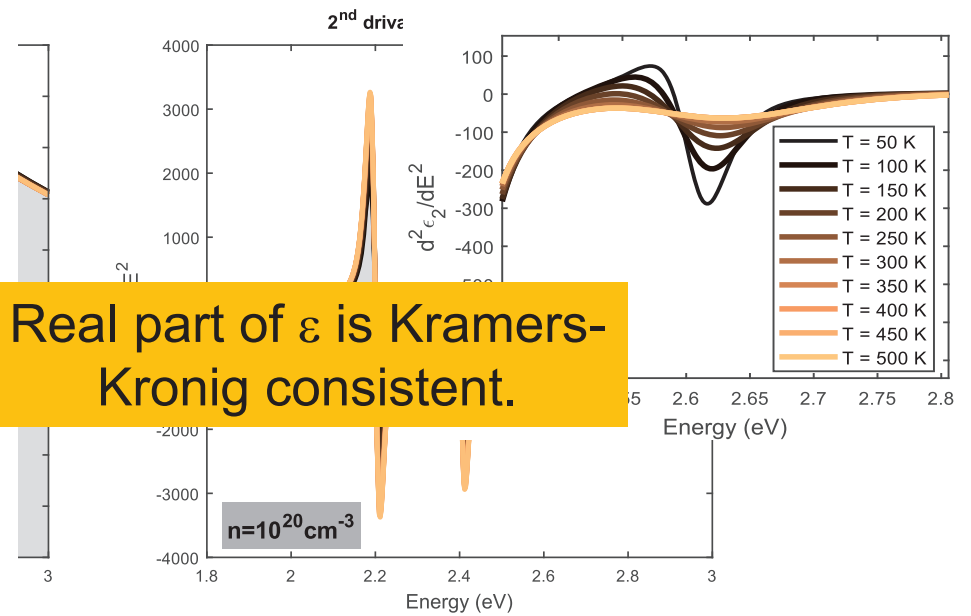
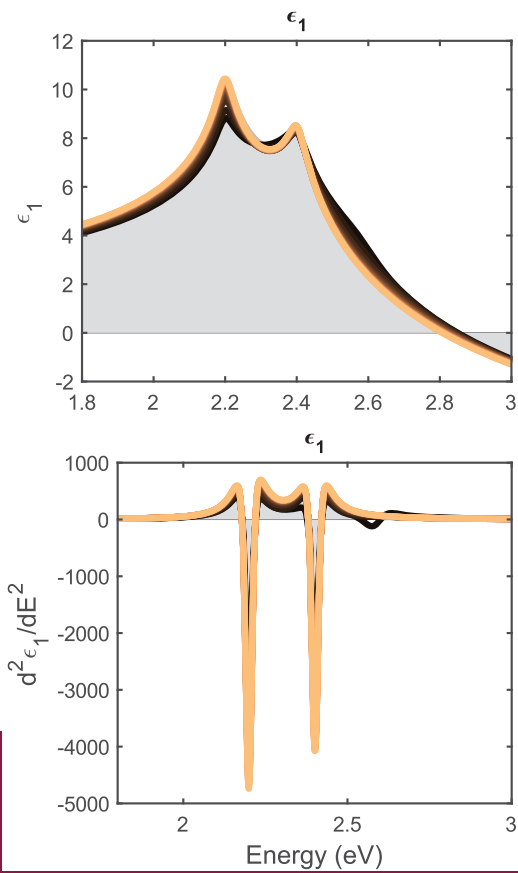
Fermi level singularity more prominent as temperature decreases.

No Burstein-Moss shift for 2D CP:
 $\Delta E_{BM} = 0$

$$\epsilon_2(E) = \frac{8e^2 \bar{P}^2 \mu_{\perp}}{3m^2 E^2} H(E - E_1) \int_{-k_{\max}}^{k_{\max}} 1 - f[E_c(E, k_z^2)] dk_z$$

Xu, JAP **125**, 085704 (2019).
 Xu, PRL **118**, 267402 (2017). 34

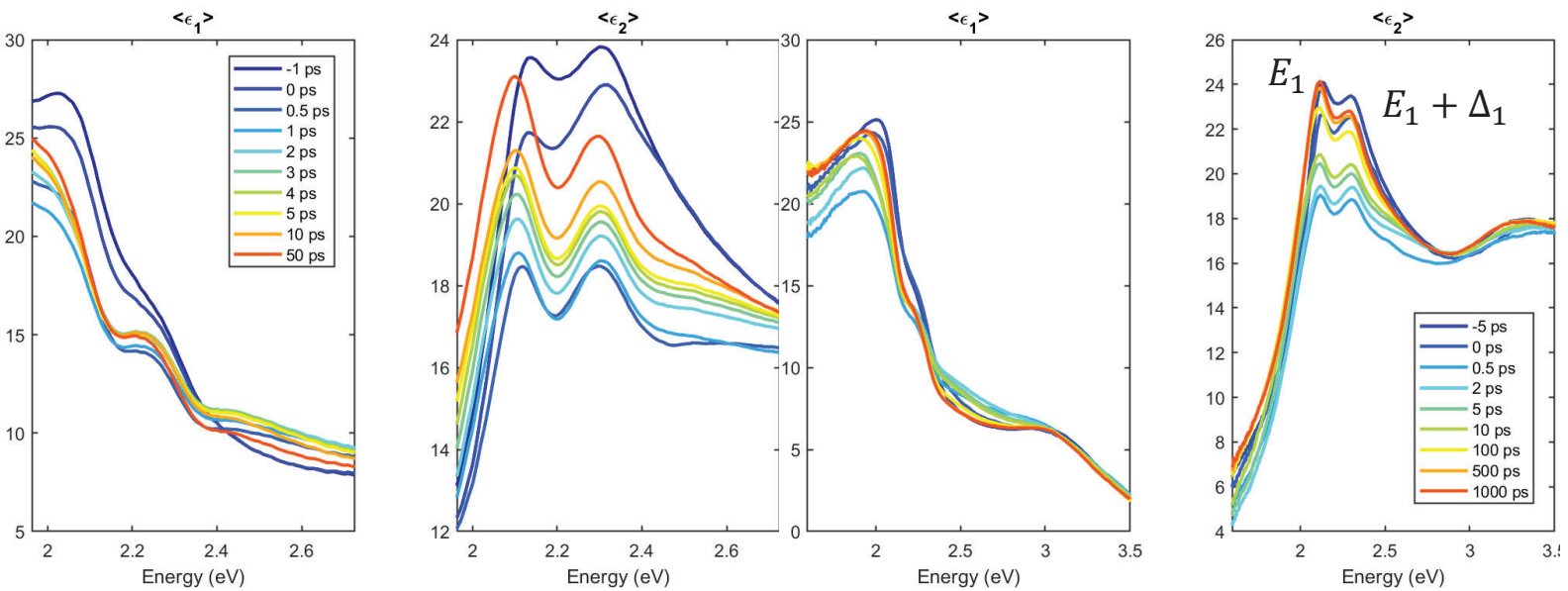
Model for transient dielectric function



ure.

Xu, JAP **125**, 085704 (2019).
Xu, PRL **118**, 267402 (2017).

Pseudo-dielectric constant as function of delay time

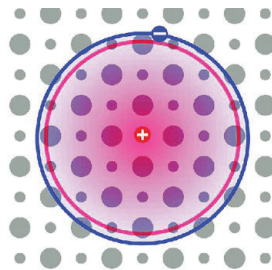
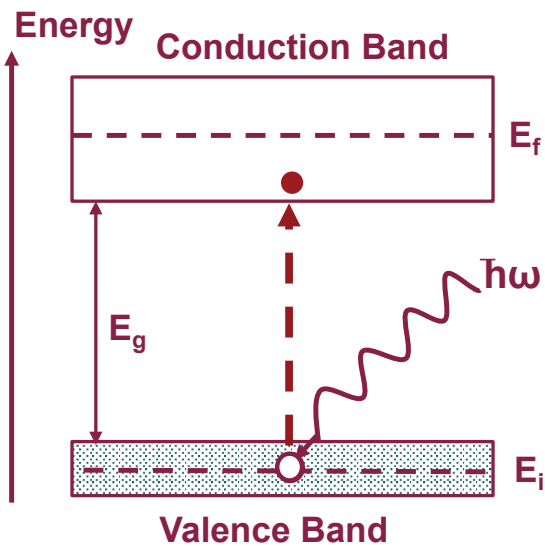


No quantitative agreement.
Need to include excitonic effects.

What have we learnt so far ?

- Calculated electron-hole concentration (about 10^{20} cm^{-3}) from Fermi-Dirac statistics.
- Electrons initially in Γ -valley, very hot electron plasma (2500 K)
- Within 50 fs, most electrons (>50%) scatter to the X-valley (large density of states).
- Electrons cool by intervalley scattering.
When $T < 1000 \text{ K}$, most electrons are in the L-valley
L-electrons are observable by bleaching the absorption of the probe pulse.
- Theory predicts a reduction of ϵ_2 due to band filling (Pauli blocking) by about 20%.
- **A reduction by 25% is observed in the experiment, but the amplitude and line shape are wrong.**
- **What is missing?**
- L-valley absorption is enhanced by excitons.
- Excitonic (Sommerfeld) enhancement is screened by high electron density.
- Next, we need to talk about **excitons**.

Exciton concept: Bound Electron-Hole Pair



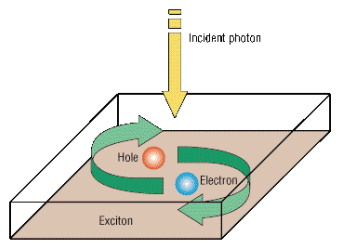
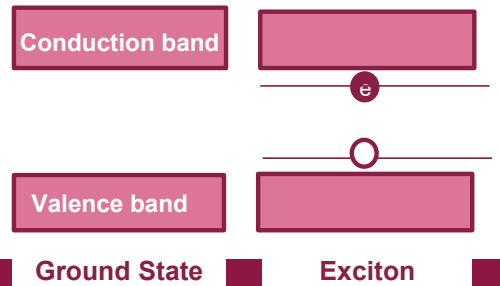
- Large radius (larger than atomic spacing)
- Weakly bound

Bohr model for exciton

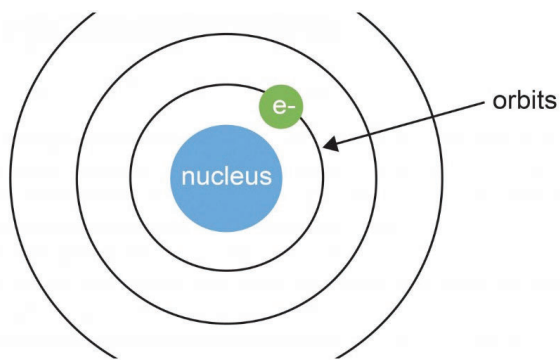
Excitons in semiconductors

	Excitonic Radius(Å)	Lattice Constant(Å)	Excitonic Binding Energy (meV)	R
GaAs	130	5.6532	4.2	
SrTiO ₃	62.5	3.9050	20	
GaP	50	5.4505	21	
ZnO	20	a=3.2500, c=5.2040	60	

Semiconductor Picture



Shape the Future.



Electron and hole form a bound state with binding energy.

$$E(n) = -\frac{\mu}{m_0} \frac{1}{\epsilon_r^2} \frac{R_H}{n^2} = -\frac{R}{n^2}$$

$R_H=13.6$ eV Rydberg energy.
QM mechanical treatment easy.

Bohr model for free excitons

1. Reduced electron/hole mass (**optical mass**) $\frac{1}{\mu} = \frac{1}{m_e} + \frac{1}{m_h}$
2. **Static screening** with static dielectric constant ϵ_r .
3. **Exciton radius:** $a_n = \frac{m_0}{\mu} \epsilon_r n^2 a_H$
 $a_H=0.53 \text{ \AA}$
4. Excitons **stable** if $R \gg kT$????
5. Exciton **momentum** is zero.
6. **Exciton enhancement important even if $R \ll kT$.**

Sommerfeld enhancement

Excitonic Rydberg energy

$$R = \frac{\mu}{m_0 \epsilon_r^2} R_H$$

Discrete states

$$E_n = E_g - \frac{1}{n^2} R_X$$

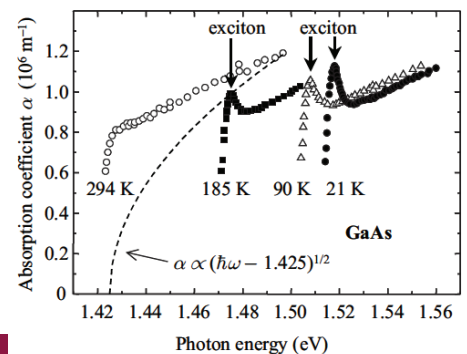
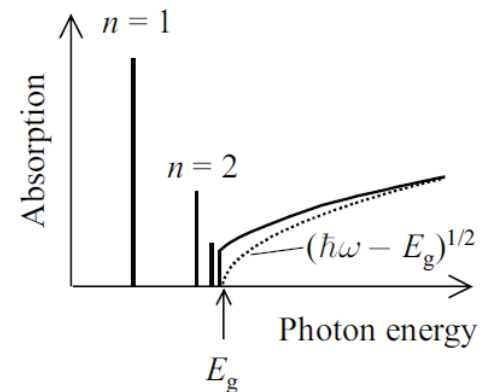
Discrete absorption

$$\epsilon_2(E) = \frac{8\pi|P|^2\mu^3}{3\omega^2(4\pi\epsilon_0)^3\epsilon_r^3} \sum_{n=1}^{\infty} \frac{1}{n^3} \delta(E - E_n)$$

Continuum absorption

$$\epsilon_2(E) = \frac{2|P|^2(2\mu)^{3/2}\sqrt{E - E_0}}{3\omega^2} \frac{\xi e^\xi}{\sinh \xi}$$

$$\xi = \pi \sqrt{R/E - E_0}$$



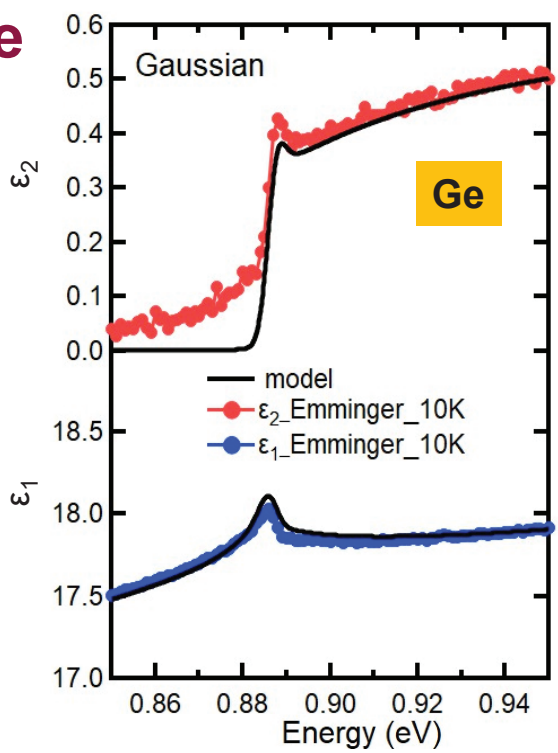
Use Bohr wave functions to calculate \$\epsilon_2\$. Toyozawa discusses broadening.

R. J. Elliott, Phys. Rev. **108**, 1384 (1957)
Yu & Cardona; Fox, Chapter 4

Elliott-Tanguy theory applied to Ge

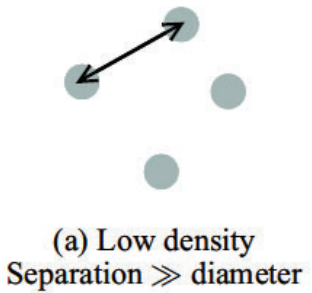
- **Fixed parameters:**
 - Electron and hole masses (temperature dependent)
 - Excitonic binding energy R
 - Amplitude A (derived from matrix element P)
- **Adjustable parameters:**
 - Broadening Γ : 2.3 meV
 - Band gap E_0
 - Linear background A_1 and B_1 (contribution from E_1 to real part of ϵ)
- **Problems:**
 - Broadening below the gap (band tail, oxide correction)

Quantitative agreement



Condensation of excitons at high density

Exciton gas



Mott transition (insulator-metal) when electron separation equals exciton radius.

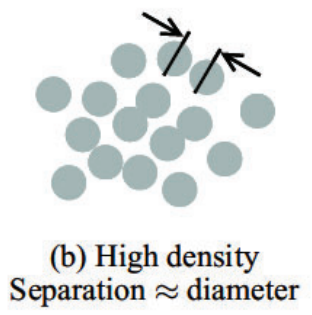
Electron separation d for density N

$$d = \sqrt[3]{\frac{3}{4\pi n}}$$

$$r_s = \frac{d}{a_X}$$

dimensionless

Electron-hole liquid



Mott transition occurs at r_s near 1.
GaAs: $n=10^{17} \text{ cm}^{-3}$.

Biexciton, triexciton molecule formation.
Electron-hole droplets. Bose-Einstein condensation.

Excitons in doped or excited semiconductors

Need to include exciton screening due to doping.

Yukawa potential: Schrödinger equation not solvable.

Use Hulthen potential as an approximation

Coulomb	$V(r) = -k \frac{1}{r}$	$k = \frac{e^2}{4\pi\epsilon_0\epsilon_r}$	Debye screening length
Yukawa	$V(r) = -k \frac{\exp(-r/\lambda_D)}{r}$	$\lambda_D = \sqrt{\frac{\epsilon_r\epsilon_0 k_B T}{ne^2}} = \frac{1}{k_D}$	
Hulthen	$V(r) = -k \frac{2/ga_X}{\exp\left(\frac{2r}{ga_X}\right) - 1}$	$g = \frac{\lambda_D}{a_X}$	Unscreened: $g=\infty$ Fully screened: $g=0$ Mott criterion: $g=1$

Hulthen exciton e Future.

C. Tanguy, Phys. Rev. **60**, 10660 (1999).
 Banyai & Koch, Z. Phys. B **63**, 283 (1986).

Tanguy: Dielectric function of screened excitons

Bound exciton states (finite number):

$$A = \frac{\hbar^2 e^2}{6\pi\epsilon_0 m_0^2} \left(\frac{2\mu}{\hbar^2} \right)^{3/2} |P|^2$$

$$\epsilon_2(\omega) = \frac{2\pi A \sqrt{R}}{E^2} \sum_{n=1}^{n^2 < g} 2R \frac{1}{n} \left(\frac{1}{n^2} - \frac{n^2}{g^2} \right) \delta \left[E - E_0 + \frac{R}{n^2} \left(1 - \frac{n^2}{g} \right)^2 \right]$$

Reduced Rydberg energy

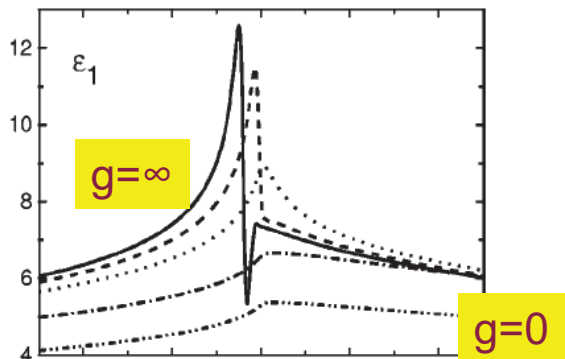
exciton continuum:

$$\epsilon_2(\omega) = \frac{2\pi A \sqrt{R}}{E^2} \frac{\sinh \pi g k}{\cosh(\pi g k) - \cosh \left(\pi g \sqrt{k^2 - \frac{4}{g}} \right)} \theta(E - E_0)$$

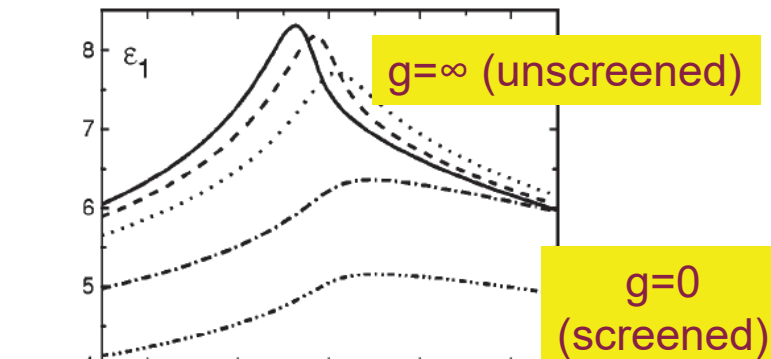
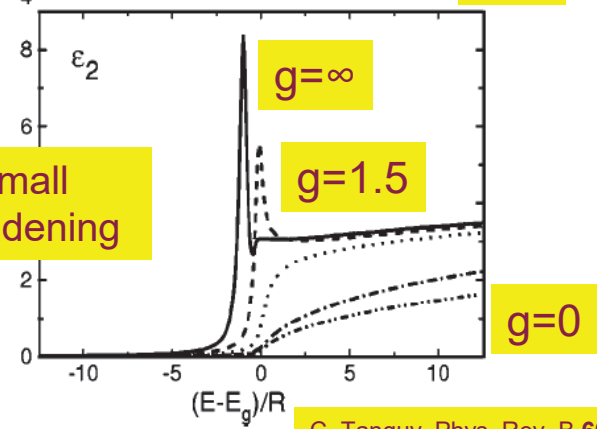
$$k = \pi \sqrt{(E - E_0)/R}$$

Need to introduce Lorentzian broadening and perform numerical KK transform.

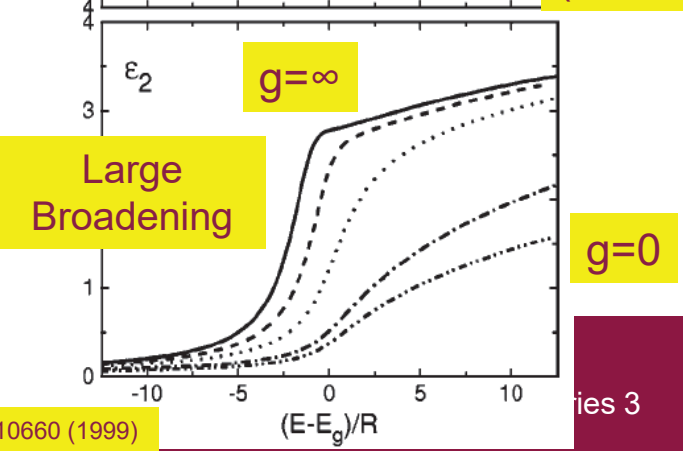
Tanguy: Dielectric function of screened excitons



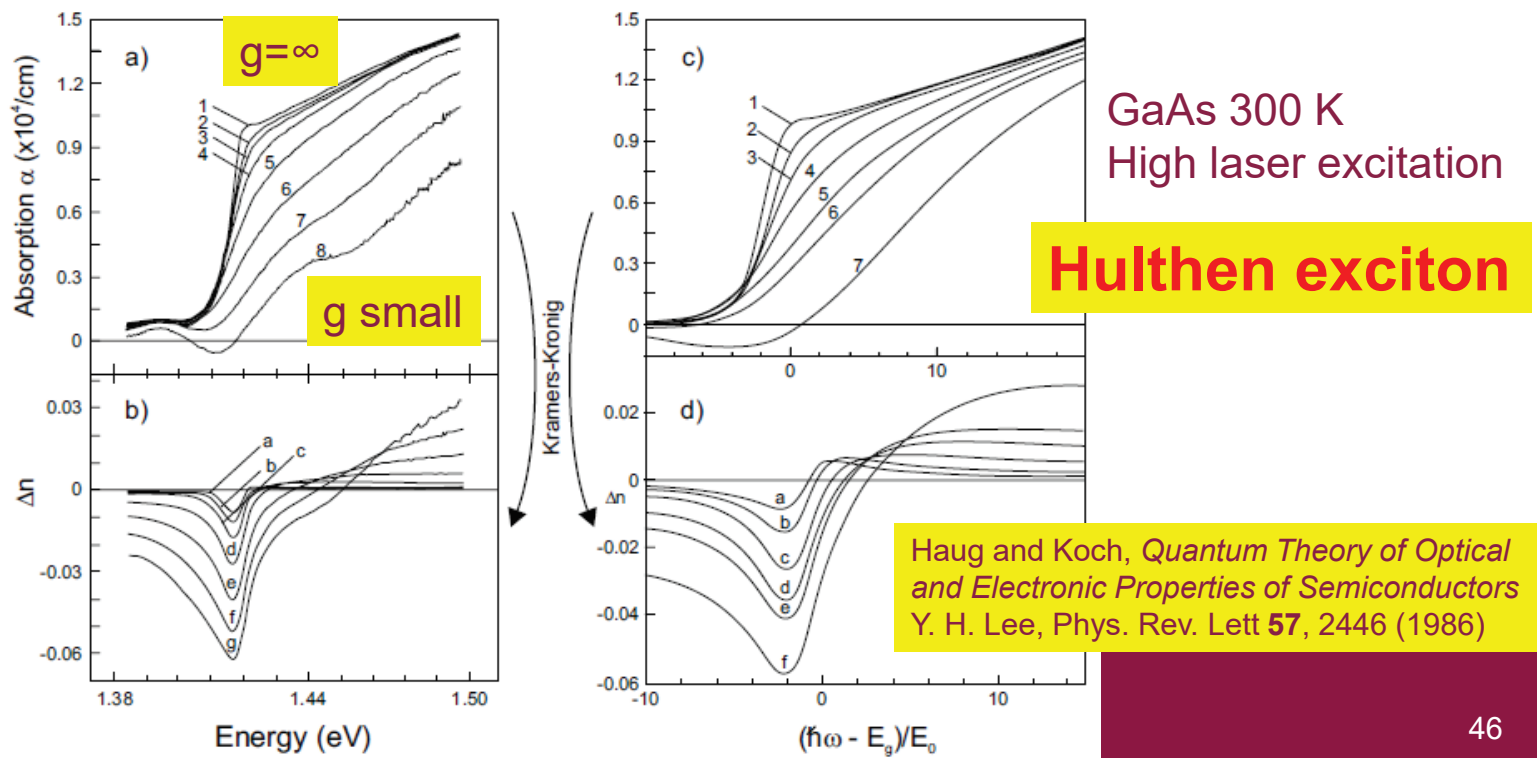
Small Broadening



Large Broadening



Excitons in laser-excited GaAs



Two-dimensional Bohr problem

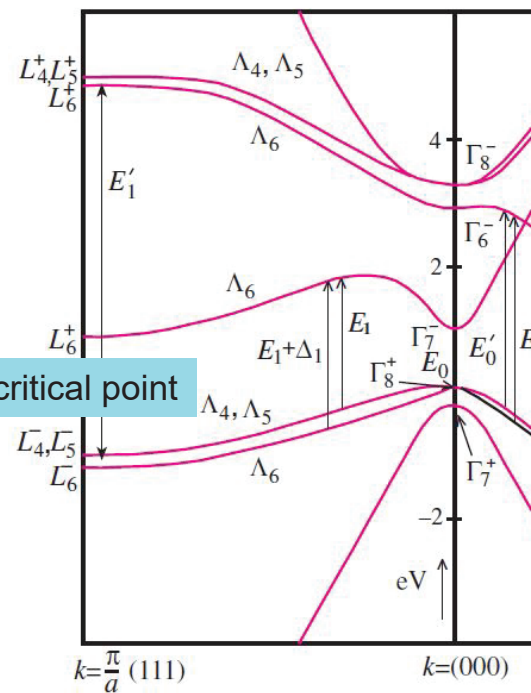
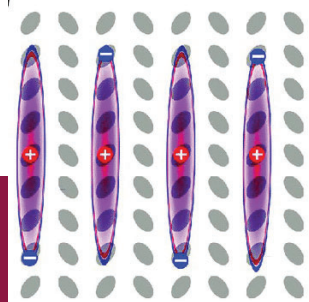
$$H = -\frac{\hbar^2}{2\mu_{\perp}} \left(\frac{\partial^2}{\partial x^2} + \frac{\partial^2}{\partial y^2} \right) - \frac{\hbar^2}{2\mu_{\parallel}} \frac{\partial^2}{\partial z^2} - \frac{e^2}{\epsilon_r r}$$

Assume that μ_{\parallel} is infinite (separate term).
 Use cylindrical coordinates.
 Separate radial and polar variables.
 Similar Laguerre solution as 3D Bohr problem.

$$a_x = \frac{4\pi\epsilon_0\epsilon_r\hbar^2 m_0}{\mu_{\perp}\mu e^2}$$

$$R = \frac{\mu_{\perp} e^4}{2\hbar^2 m_0 (4\pi\epsilon_0\epsilon_r)^2}$$

$$E_n = -\frac{R}{\left(n - \frac{1}{2}\right)^2}, \quad n = 1, 2, \dots$$



Half-integral quantum numbers
 STATE BE BOLD. Shape the Future.

M. Shinada and S. Sugano, J. Phys. Soc. Jpn. 21, 1936 (1966).

Two-dimensional saddle-point excitons ($E_1, E_1 + \Delta_1$)

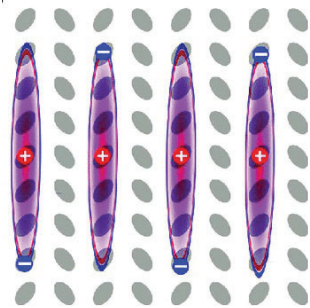
$$\varepsilon(E) = \frac{A}{(E + i\Gamma)^2} \{g[\xi(E + i\Gamma)] + g[\xi(-E - i\Gamma)] - 2g[\xi(0)]\}$$

$$g(\xi) = 2\ln(\xi) - 2\psi\left(\frac{1}{2} - \xi\right)$$

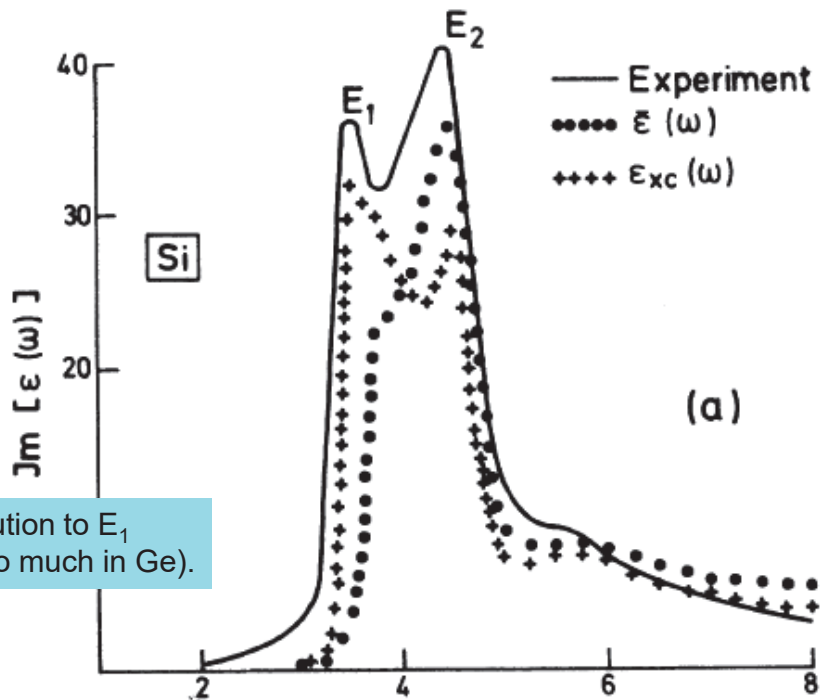
$$\psi(z) = \frac{d\ln\Gamma(z)}{dz}$$

$$\xi(z) = \sqrt{R/E_0 - z}$$

$$A = \frac{\mu e^2}{3\pi\varepsilon_0 m_0^2} |P|^2$$



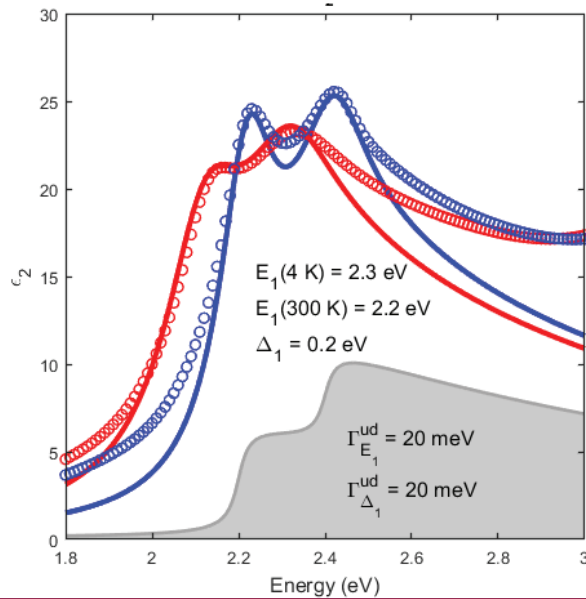
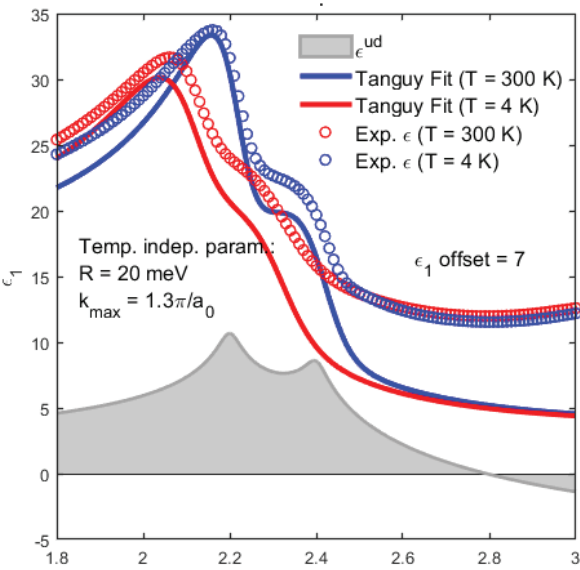
Strong excitonic contribution to E_1 critical point in Si (not so much in Ge).



- B. Velicky and J. Sak, *phys. status solidi* **16**, 147 (1966)
- C. Tanguy, *Solid State Commun.* **98**, 65 (1996)
- W. Hanke and L.J. Sham, *Phys. Rev. B* **21**, 4656 (1980)

Comparison with experimental data

$$\varepsilon(E, E_1, \Gamma, R, k_{\max}) = \frac{k_{\max} e^2 \bar{P}^2 \mu_{\perp}^{(E_1)}}{3 \varepsilon_0 m^2 \pi (E + i\Gamma)^2} \left\{ g_a \left[\sqrt{\frac{R}{E_1 - (E + i\Gamma)}} \right] + g_a \left[\sqrt{\frac{R}{E_1 - (-E - i\Gamma)}} \right] - 2g_a \left[\sqrt{\frac{R}{E_1 - (0)}} \right] \right\}$$



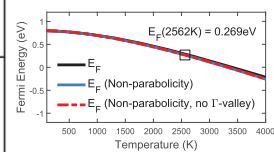
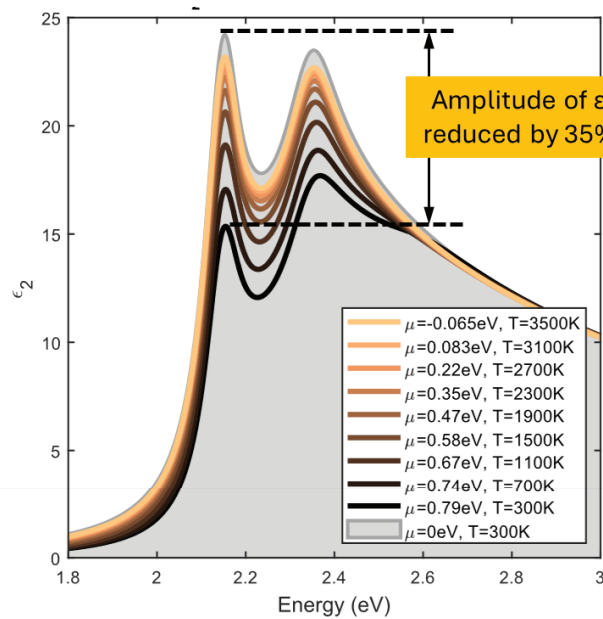
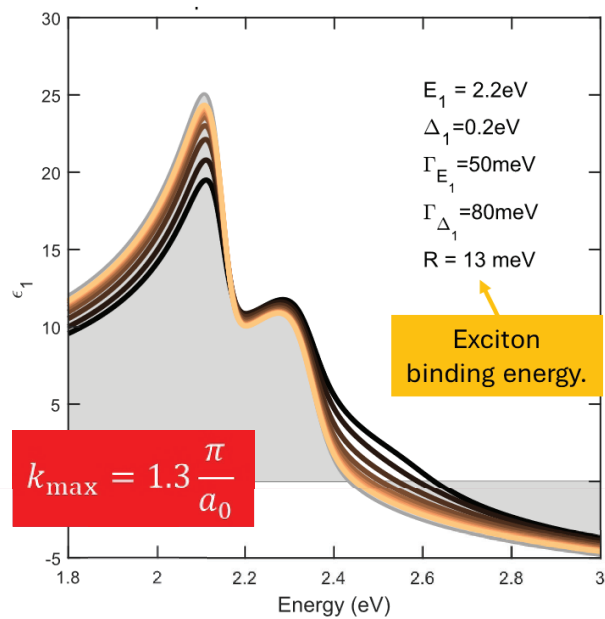
Experimental data:

Emminger (5 K),
 JVST B **38**,
 012202 (2020).

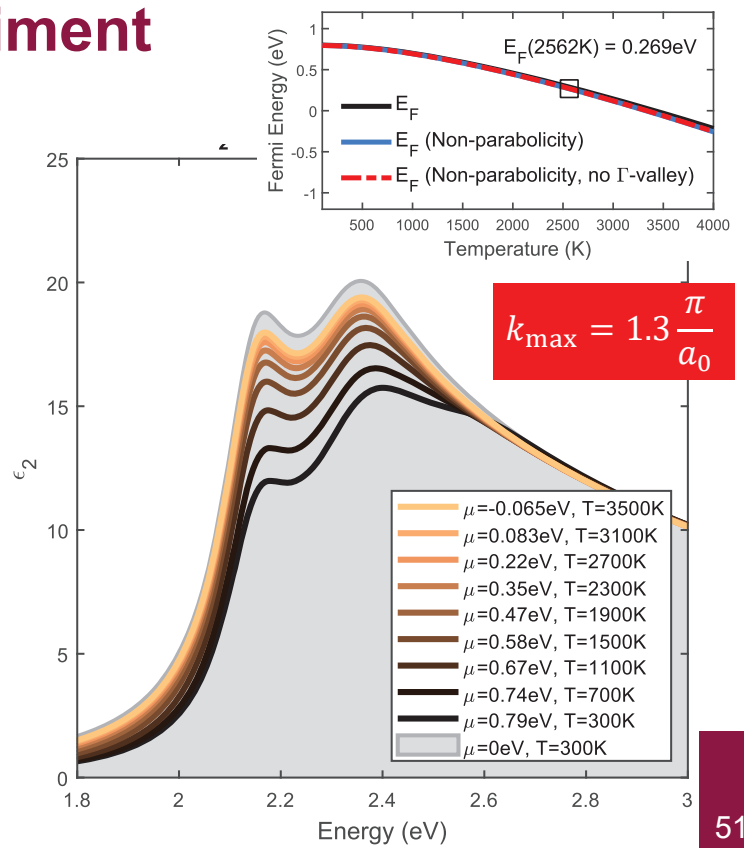
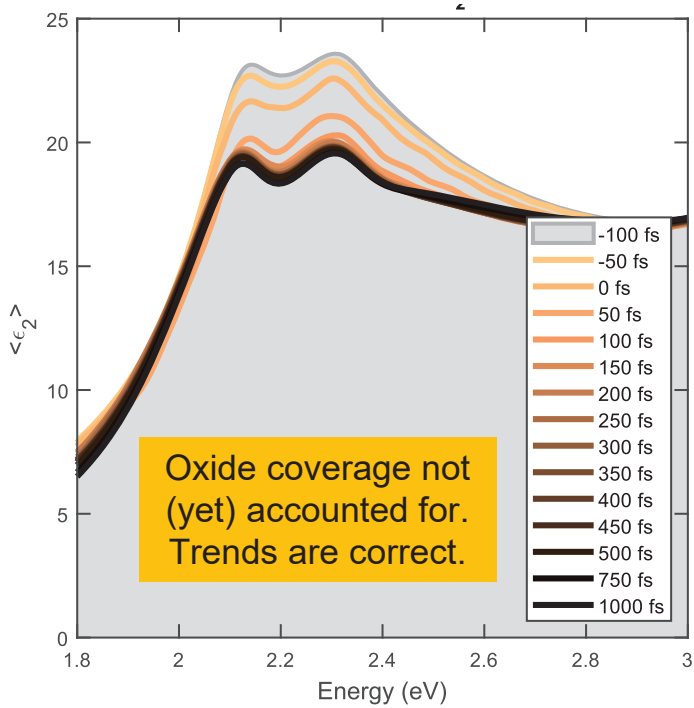
Nunley (300 K),
 JVST B **34**,
 061205 (2016)

2D excitons with band filling ($E_1, E_1 + \Delta_1$)

$$\epsilon_2(E) = \frac{e^2 \mu_{\perp}^{(E_1)} \bar{p}^2}{6 \epsilon_0 m^2 \pi} \text{Im} \left\{ \frac{\{g_a[\xi(E + i\Gamma)] + g_a[\xi(-E - i\Gamma)] - 2g_a[\xi(0)]\}}{(E + i\Gamma)^2} \right\} \int_{-k_{\max}}^{k_{\max}} \{1 - f[E_c(E, k_z^2)]\} dk_z$$



Comparison with experiment



Conclusions

- Calculated electron-hole concentration (about 10^{20} cm^{-3}) from Fermi-Dirac statistics.
- Electrons initially in Γ -valley, very hot electron plasma (2500 K)
- Within 50 fs, most electrons (>50%) scatter to the X-valley (large density of states).
- Electrons cool by intervalley scattering.
When $T < 1000 \text{ K}$, most electrons are in the L-valley
L-electrons are observable by bleaching the absorption of the probe pulse.
- Theory predicts a reduction of ϵ_2 due to band filling (Pauli blocking) by about 20%.
- **A reduction by 25% is observed in the experiment, but the amplitude and line shape are wrong.**
- **Low-density dielectric function can be modeled by 2D-excitons.**
- **Band filling effects are in good agreement with transient dielectric function.**
- **What is missing?**
- **Excitonic (Sommerfeld) enhancement is screened by high electron density (TBD).**



Thank you!

Questions?

**Many students
contributed to
this project.**

<http://femto.nmsu.edu>